

CSCI 210: Computer Architecture

Lecture 12: Procedures & The Stack

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CS History: IBM System 360



- Family of mainframes developed in 1964
- Introduced:
 - 8-bit byte
 - Byte-addressable memory
 - 32-bit words
- Featured BAL (Branch and Link) and BR (Branch Register) instructions
- IBM's current System z mainframes will still run code written for the 360 series

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Register values across function calls

- “Preserved” registers
 - You can trust them to persist past function calls
 - Functions must ensure not to change them or to restore them if they do
- Not “Preserved” registers
 - Contents can be changed when you call a function
 - If you need the value, you need to put it somewhere else

Aside: MIPS Register Convention

Name	Register Number	Usage	Preserve on call?
\$zero	0	constant 0 (hardware)	n.a.
\$at	1	reserved for assembler	n.a.
\$v0 - \$v1	2-3	returned values	no
\$a0 - \$a3	4-7	arguments	no
\$t0 - \$t7	8-15	temporaries	no
\$s0 - \$s7	16-23	saved values	yes
\$t8 - \$t9	24-25	temporaries	no
\$gp	28	global pointer	yes
\$sp	29	stack pointer	yes
\$fp	30	frame pointer	yes
\$ra	31	return addr (hardware)	yes

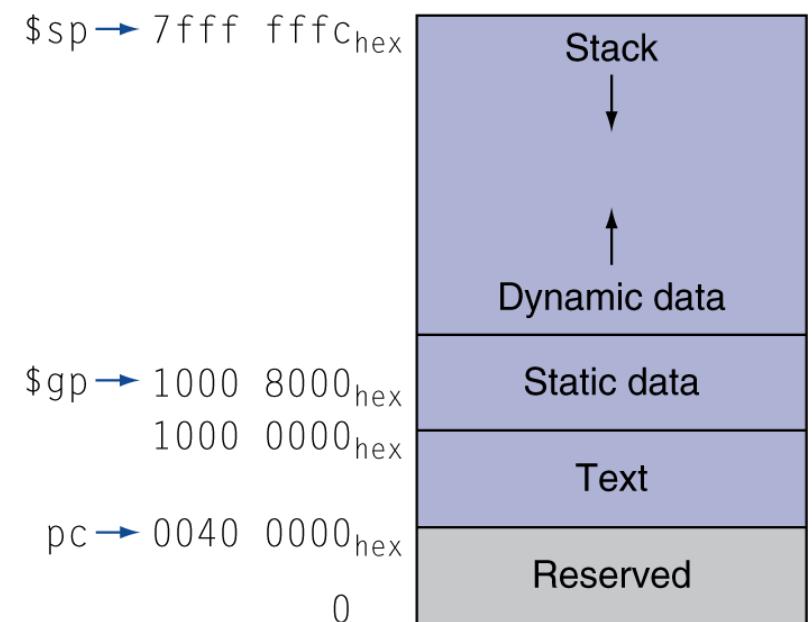
Programmer's responsibility

“Spill” and “Fill”

- Spill register **to** memory
 - Whenever you have too many variables to keep in registers
 - Whenever you call a method and need values in non-preserved registers
 - Whenever you want to use a preserved register and need to keep a copy
- Fill registers **from** memory
 - To restore previously spilled registers

Memory Layout

- Text: program code
- Static data: global variables
 - e.g., static variables in C, constant arrays and strings
- Dynamic data: heap
 - E.g., malloc in C, new in Java
- Stack: “automatic” storage for procedures



Before and after a function

Assembly Code

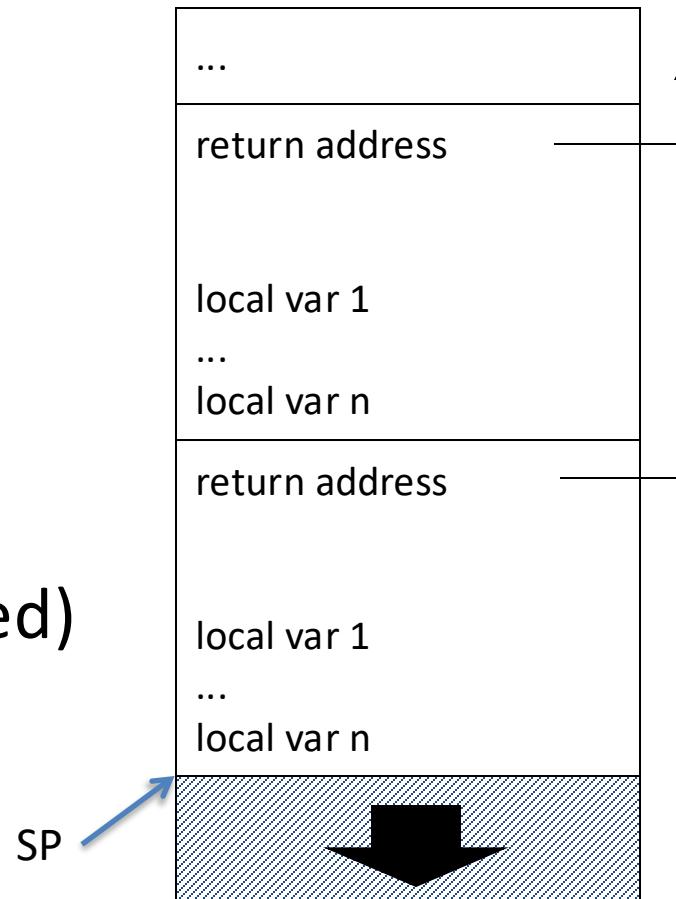
```
sw    $t0, 4($sp)
jal   myFunction
lw    $t0, 4($sp)
```

Which register is being spilled and filled?

- A. \$ra
- B. \$t0
- C. \$sp
- D. No register is spilled/filled
- E. No need to spill/fill any registers

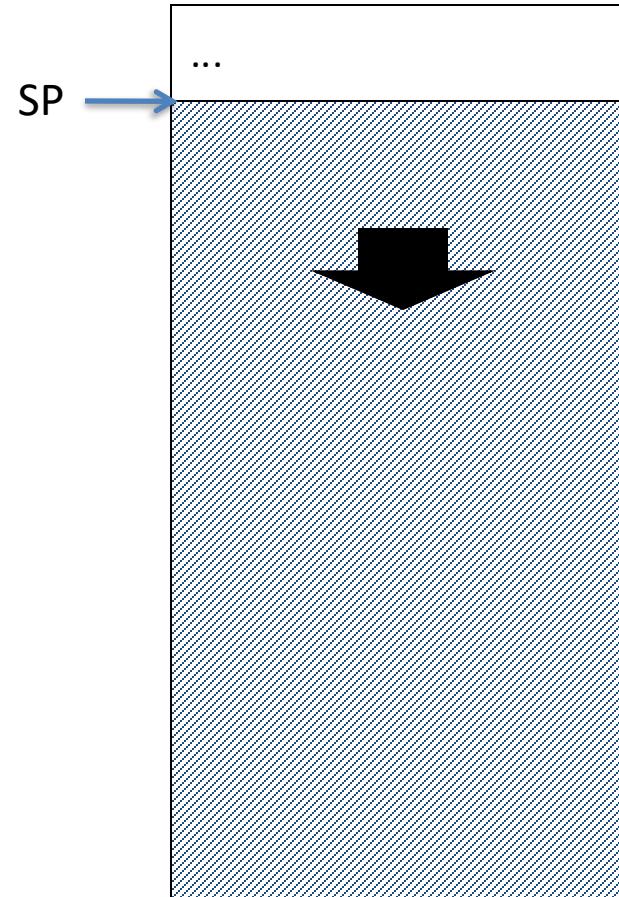
Stack

- Stack of stack frames
 - One per pending procedure
- Each stack frame stores
 - Where to return to
 - Local variables
 - Arguments for called functions (if needed)
- Stack pointer points to last record

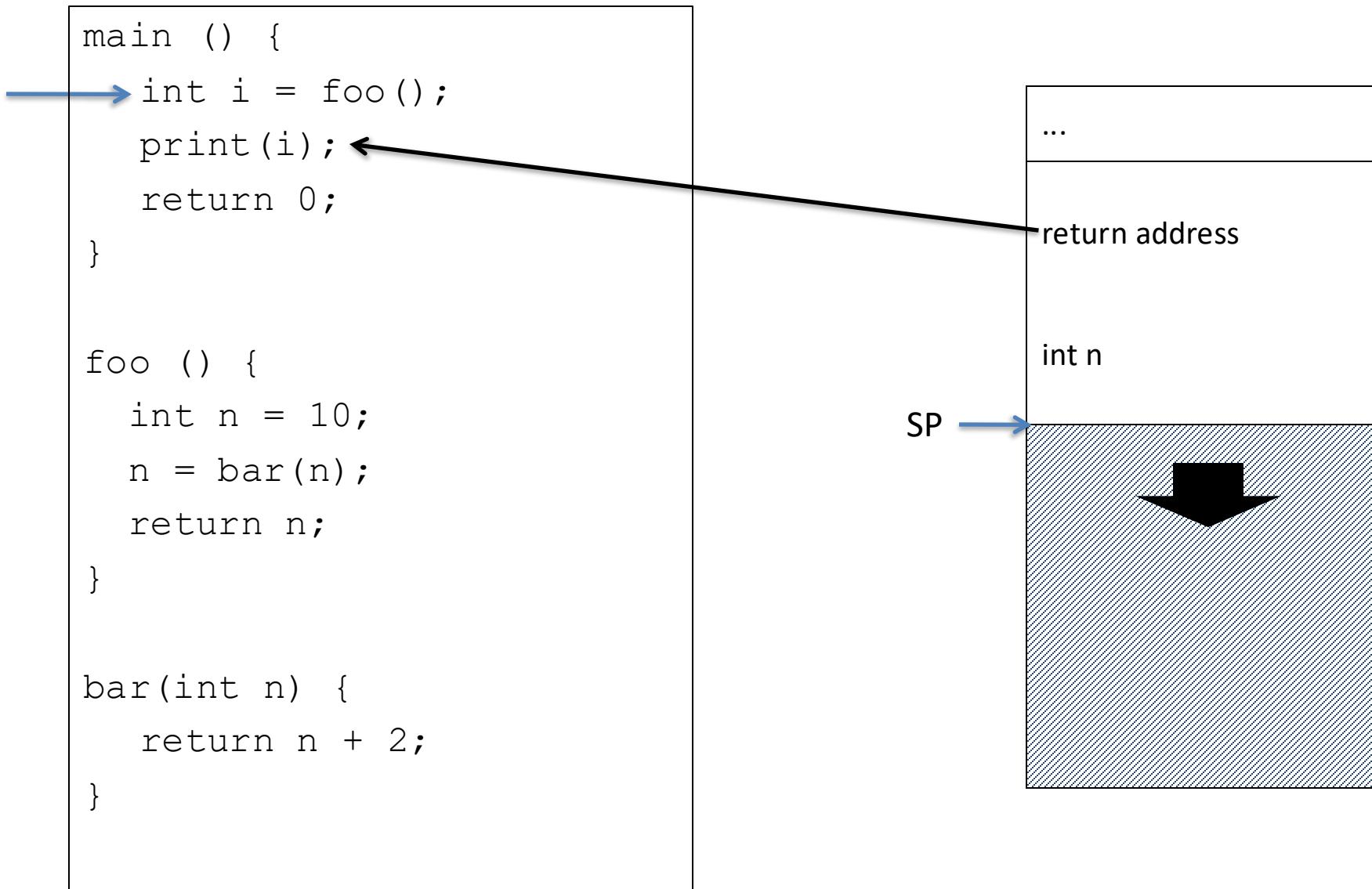


Process Stack

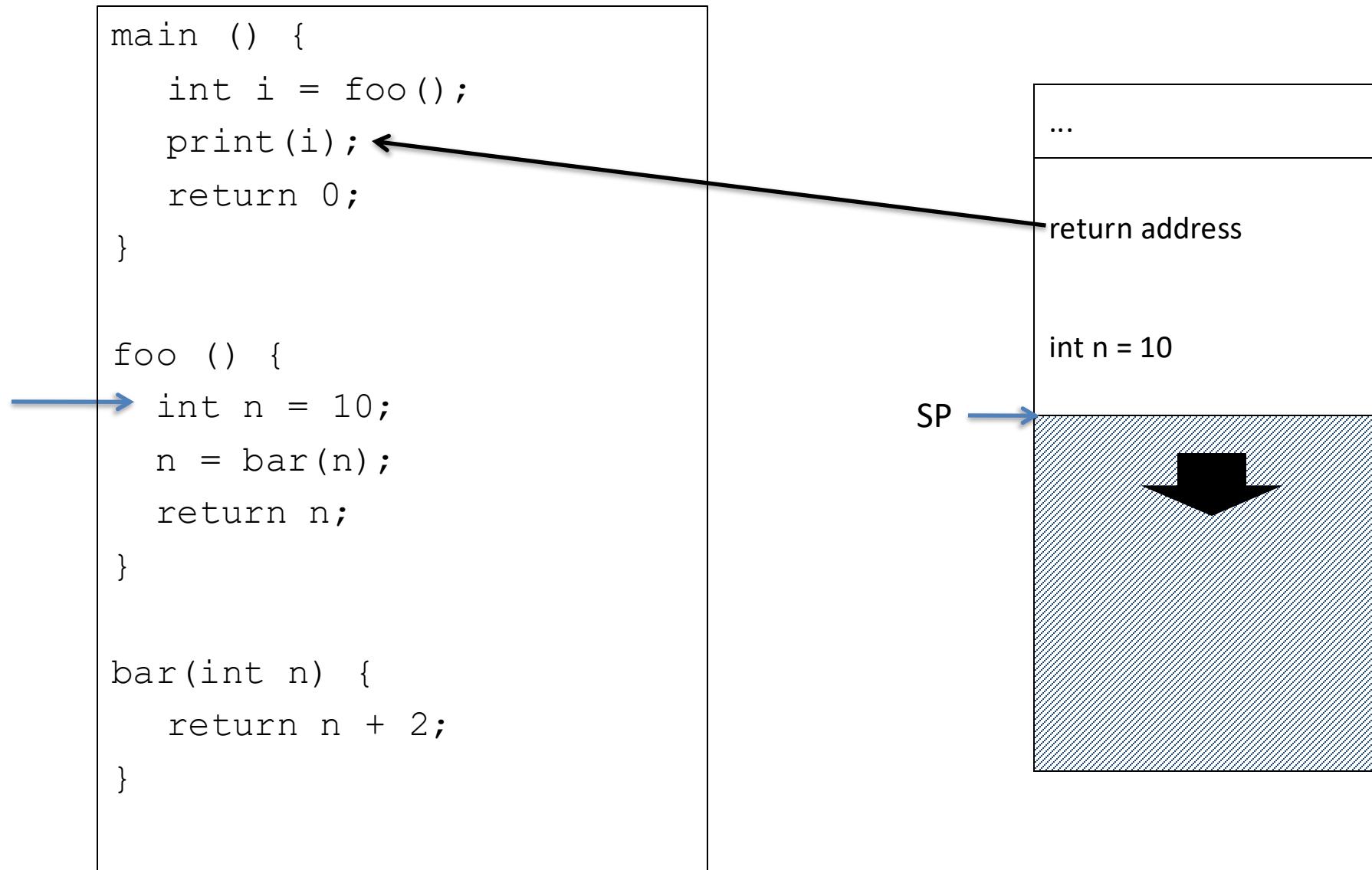
```
main () {  
    int i = foo();  
    print(i);  
    return 0;  
}  
  
foo () {  
    int n = 10;  
    n = bar(n);  
    return n;  
}  
  
bar(int n) {  
    return n + 2;  
}
```



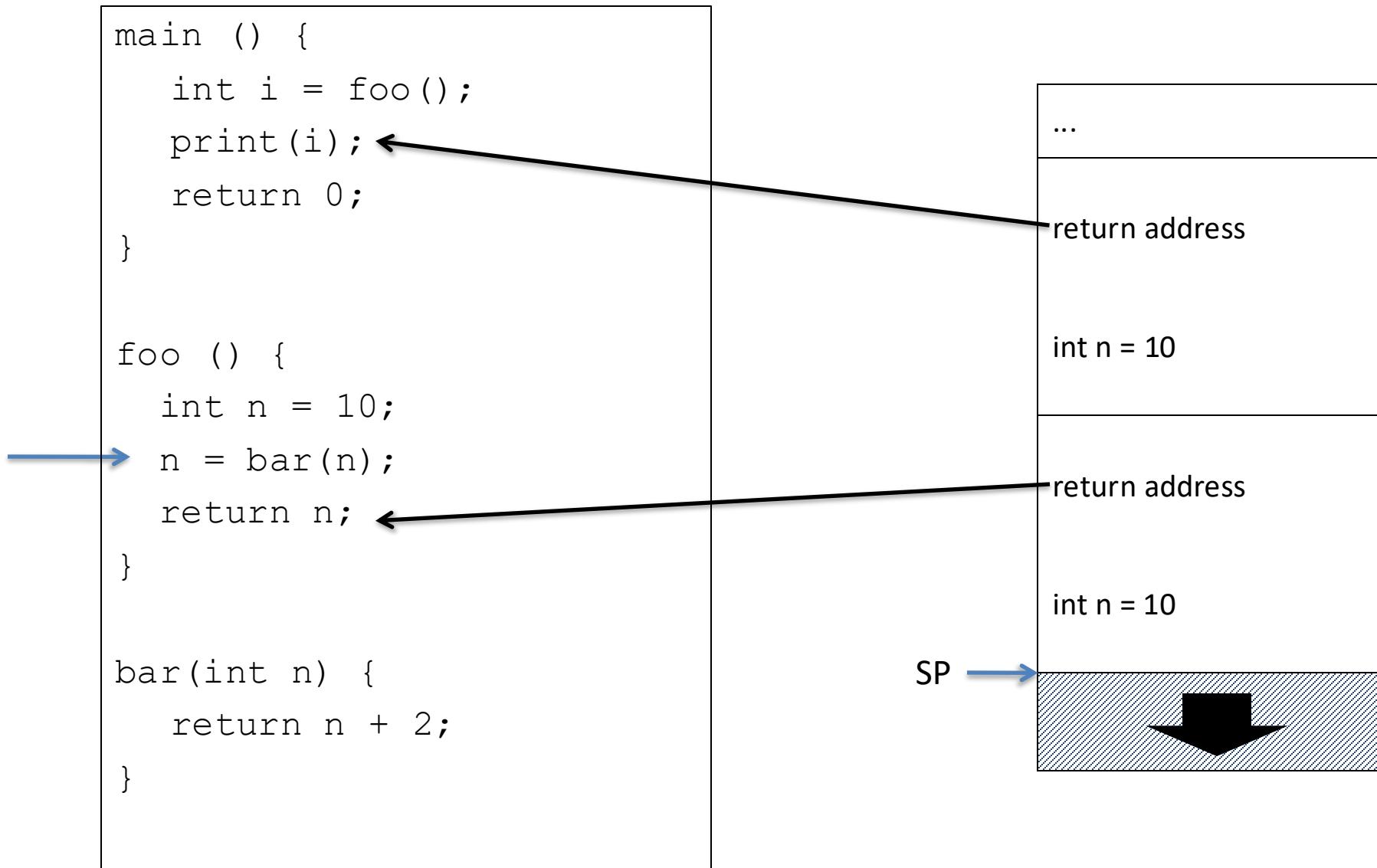
Process Stack



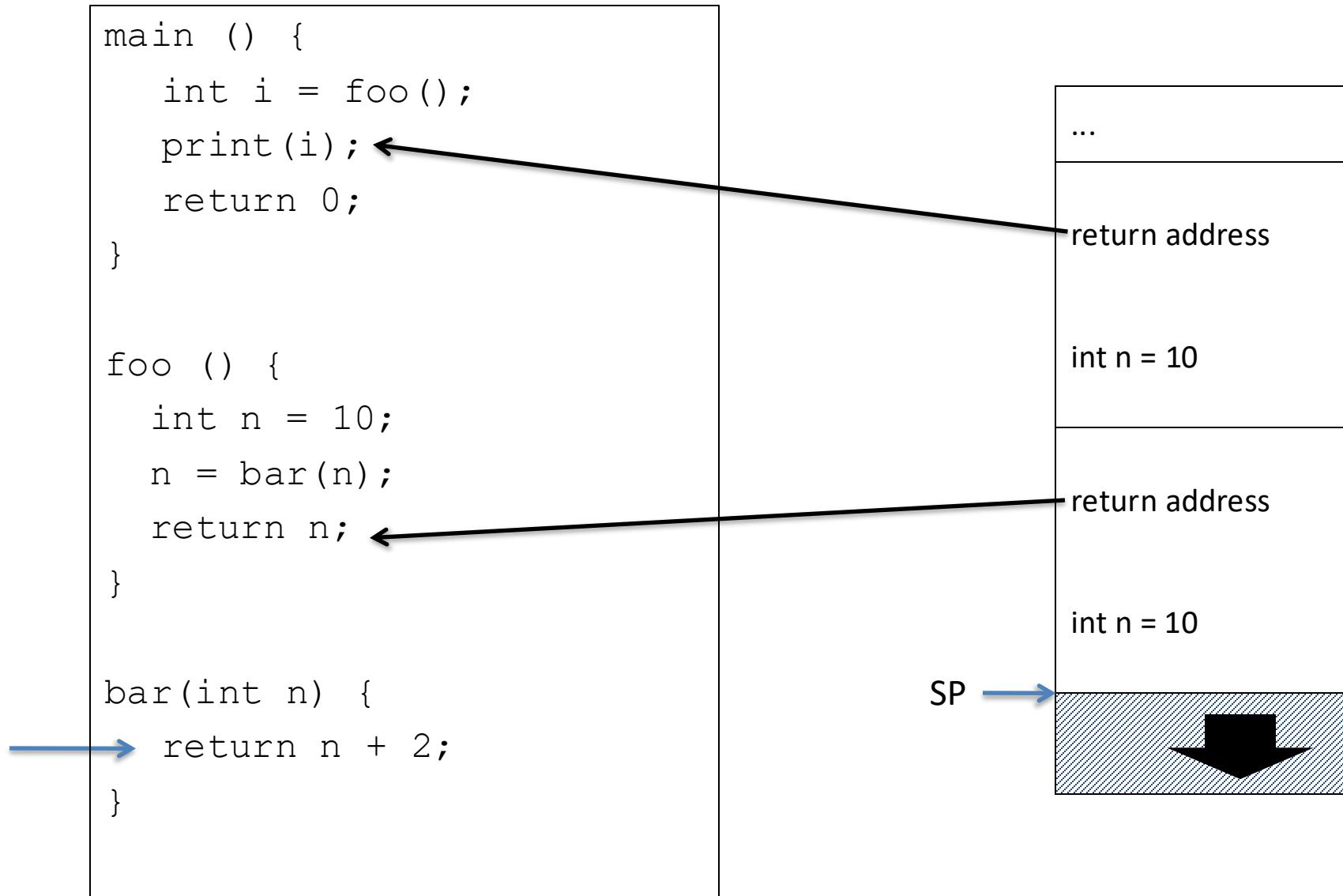
Process Stack



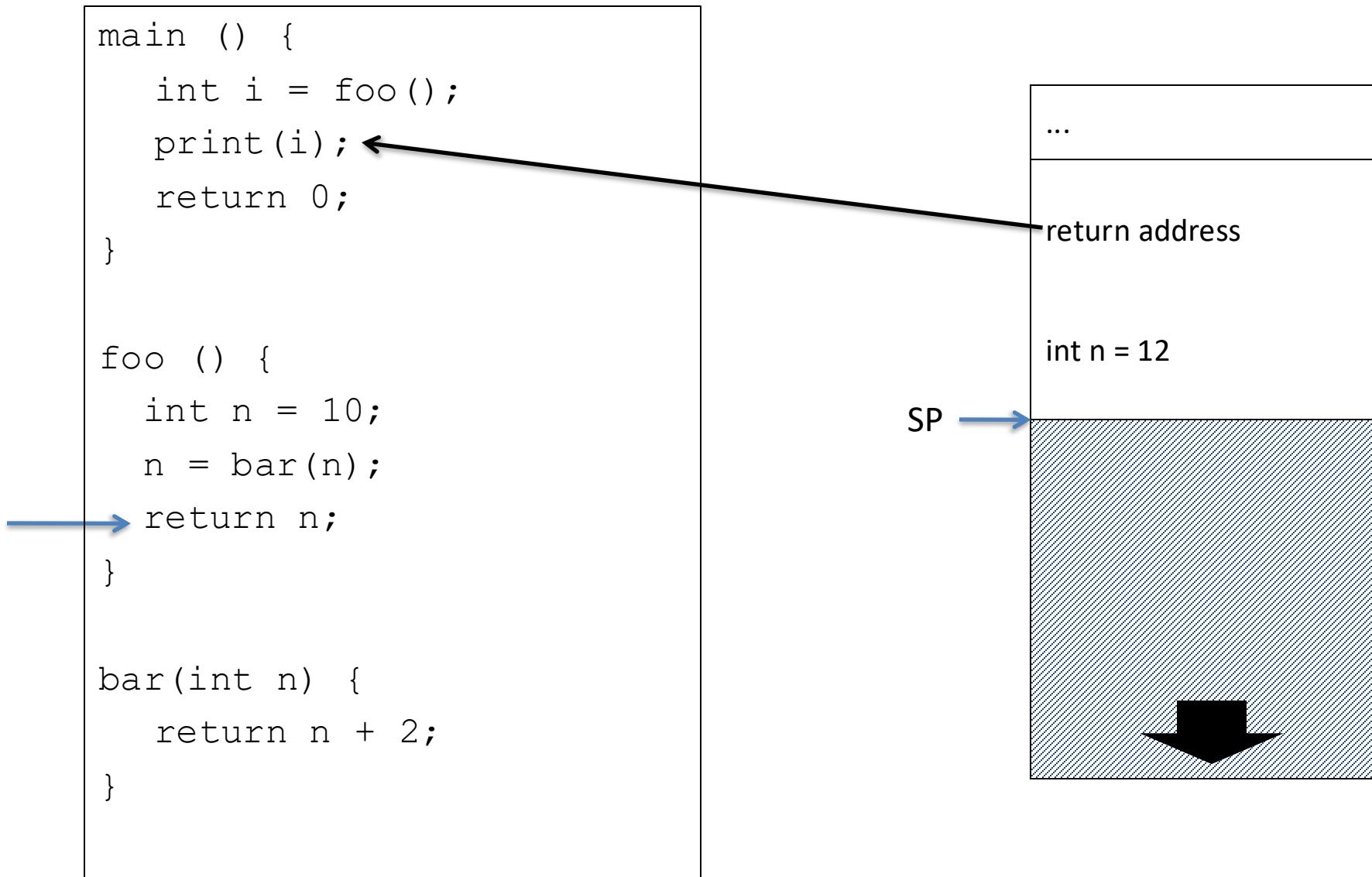
Process Stack



Process Stack

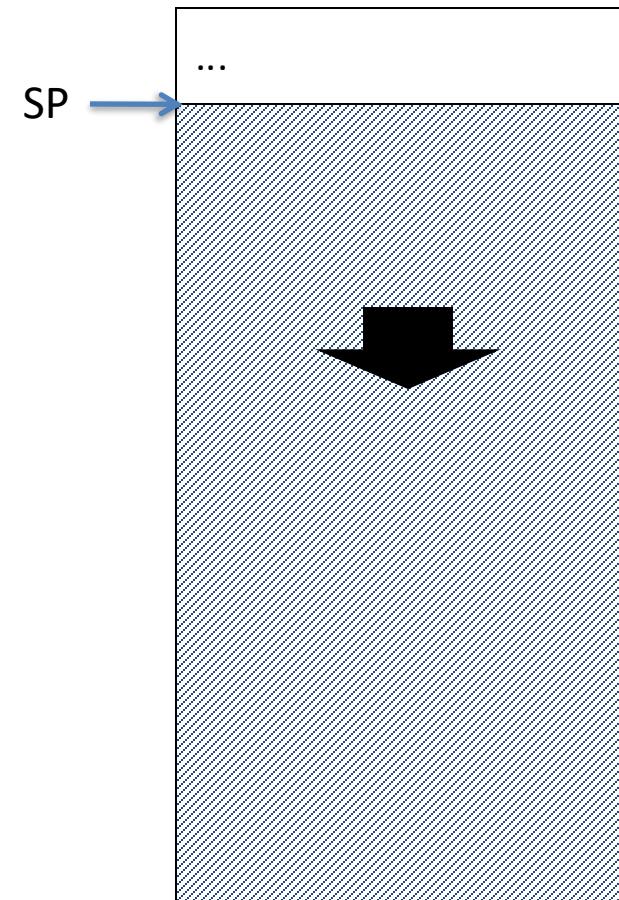


Process Stack



Process Stack

```
main () {  
    int i = foo();  
    print(i);  
    return 0;  
}  
  
foo () {  
    int n = 10;  
    n = bar(n);  
    return n;  
}  
  
bar(int n) {  
    return n + 2;  
}
```



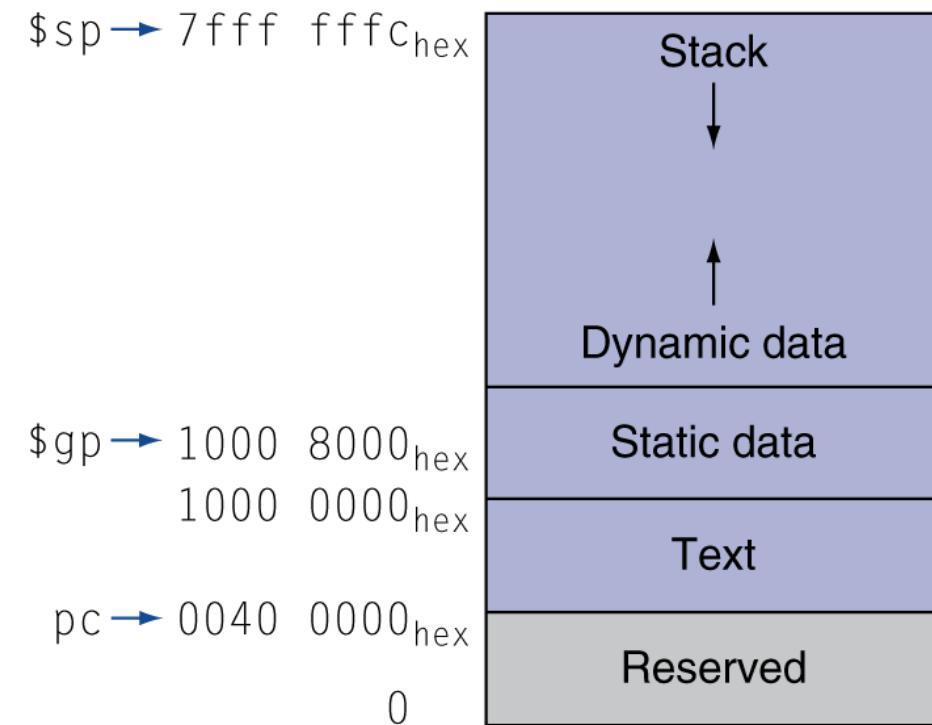
To add a variable to the stack in MIPS

- Change the stack pointer \$sp to create room on the stack for the variable
- Use sw to store the variable on the stack
- The stack pointer in MIPS points after the last stack slot so the valid slots to access are 4(\$sp), 8(\$sp), 12(\$sp), etc.

Stack

If you wish to **push** an integer variable to the top of the stack, which of the following is true:

- A. You should decrement the stack pointer (\$sp) by 1
- B. You should decrement \$sp by 4
- C. You should increment \$sp by 1
- D. You should increment \$sp by 4
- E. None of the above



Manipulating the Stack

- To add the contents of \$s0 to the stack
 - addi \$sp, \$sp, -4
sw \$s0, 4(\$sp) ; The stack pointer points after the last stack slot
- To get the value back from the stack
 - lw \$s0, 4(\$sp)
- To “erase” the value from the stack
 - addi \$sp, \$sp, 4

Think-Pair-Share: Why do we spill and fill the return address when we call a function from inside another function?

```
func1:  
    . . .  
    addi $sp, $sp, -4  
    sw   $ra, 4($sp)  
    jal  func2  
    lw   $ra, 4($sp)  
    addi $sp, $sp, 4  
    . . .  
    jr $ra
```

A better approach

- In the function “prologue,” reserve space on the stack for all of the variables and saved registers you’ll need
- Use `sw/lw` to spill and fill as needed to the space reserved in the prologue
- In the function “epilogue,” restore any saved registers you need and update the stack pointer

Complete example

foo:

```
addi    $sp, $sp, -12 # Reserve space for 3 vars
sw      $ra, 12($sp) # Stores (spills) $ra, return address
sw      $s0, 8($sp)  # Stores (spills) s0, callee-saved reg
...
li      $s0, 25       # Set s0 to 25
sw      $t3, 4($sp)  # Stores (spills) t3, caller-saved reg
add    $a0, $t1, $t3
jal   myFunction
lw      $t3, 4($sp)  # Restores (fills) t3
...
lw      $s0, 8($sp)  # Restores (fills) s0, must restore
lw      $ra, 12($sp) # Restores (fills) $ra, return address
addi   $sp, $sp, 12   # Restore the stack pointer
jr      $ra           # Return
```

Leaf function

- If the function doesn't call any other functions, it's a "leaf"
- If a leaf function doesn't need to use any of the callee-saved registers (e.g., \$s0–\$s7), then it doesn't need to change the stack pointer or spill/fill \$ra
- Example:

```
# myFunction(int a0, int a1, int a2)  
myFunction:
```

```
    add    $t0, $a0, $a2  
    sub    $v0, $t0, $a1  
    jr    $ra
```

Leaf Procedure Example

```
int leaf_example(  
    int g, int h, int i, int j  
) {  
    int f = (g + h) - (i + j);  
    return f;  
}
```

- Arguments g, ..., j in \$a0, ..., \$a3
- Result in \$v0

```
leaf_example:  
    add    $t0, $a0, $a1  
    add    $t1, $a2, $a3  
    sub    $v0, $t0, $t1  
    jr    $ra
```

Non-Leaf Procedures

- Procedures that call other procedures
- For nested call, caller needs to save on the stack:
 - Its return address
 - Any arguments and temporaries needed after the call
- Restore from the stack after the call

Non-Leaf Procedure Example

- C code:

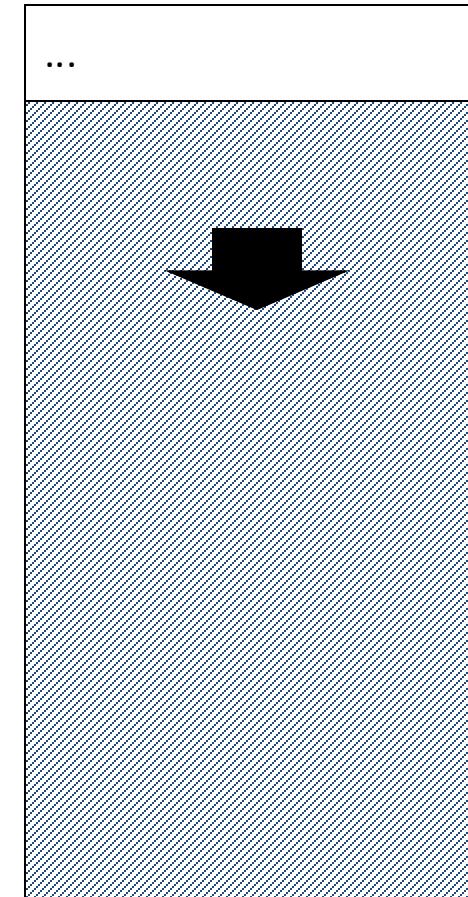
```
int fact (int n) {  
    if (n < 2)  
        return 1;  
    else  
        return n * fact(n - 1);  
}
```

- Argument n in \$a0
- Result in \$v0

Process Stack

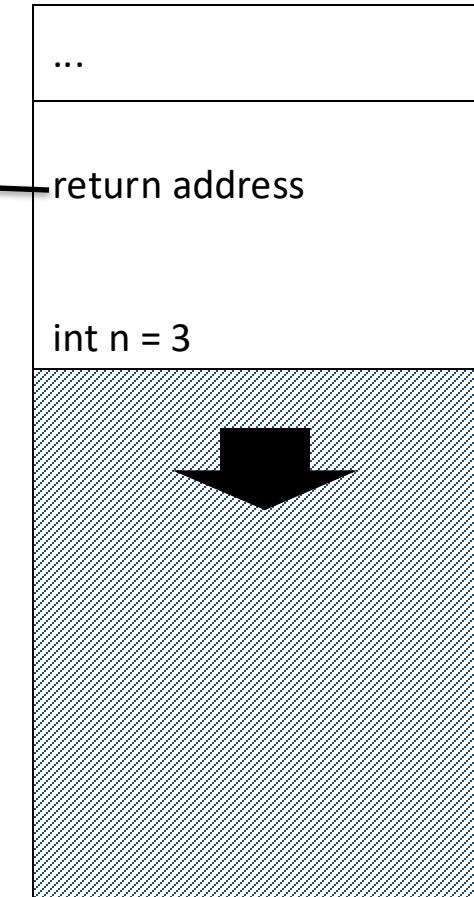
```
int main ()
{
    int x;
    x = fact(3);
}

int fact (int n)
{
    if (n < 2)
        return 1;
    else
        return n * fact(n - 1);
}
```



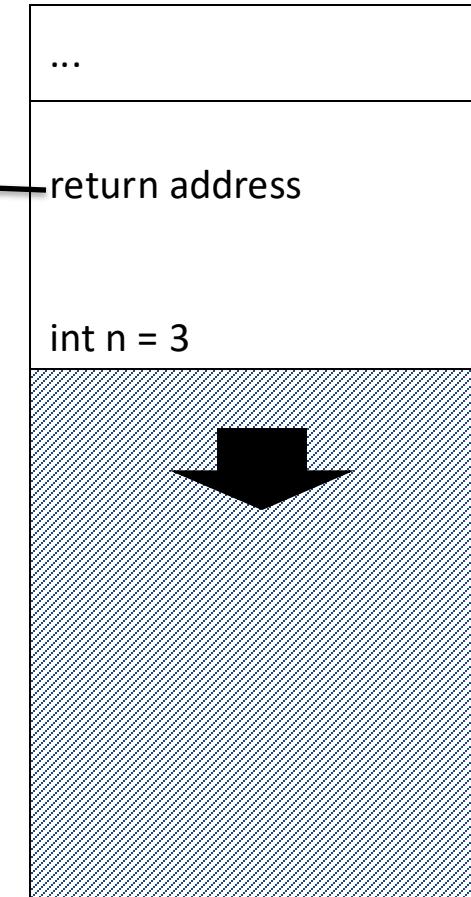
Process Stack

```
int main ()  
{  
    int x;  
    x = fact(3); ←  
}  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        return n * fact(n - 1);  
}
```

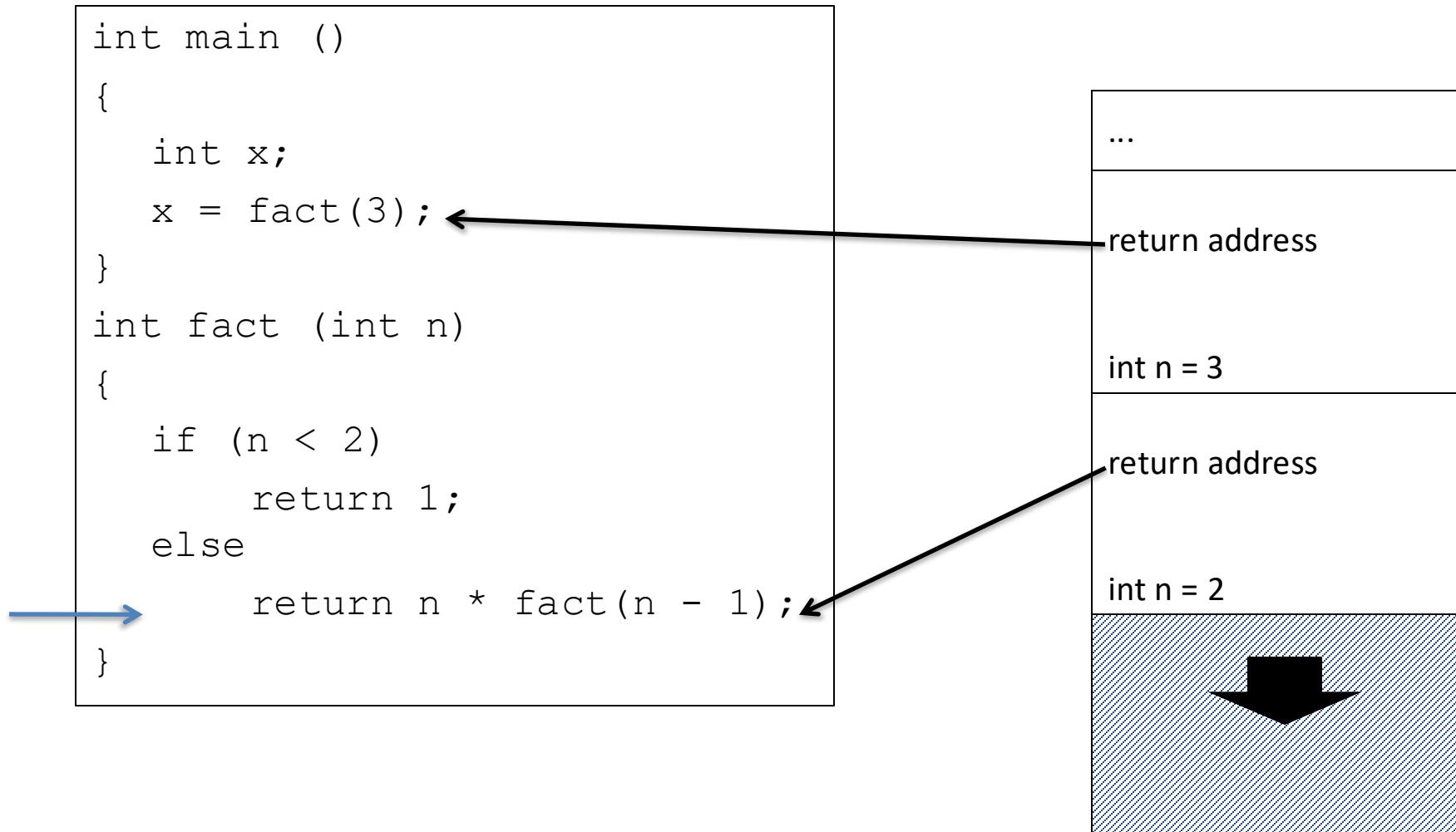


Process Stack

```
int main ()  
{  
    int x;  
    x = fact(3); ←  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        return n * fact(n - 1);  
}
```

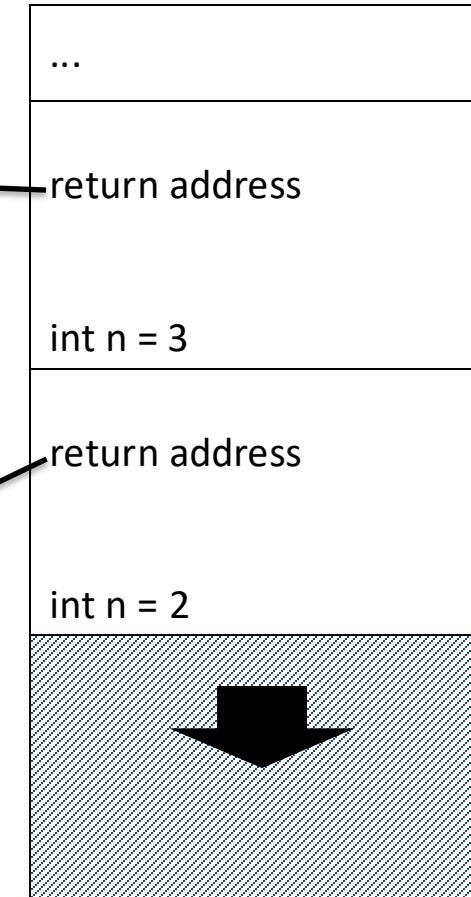


Process Stack

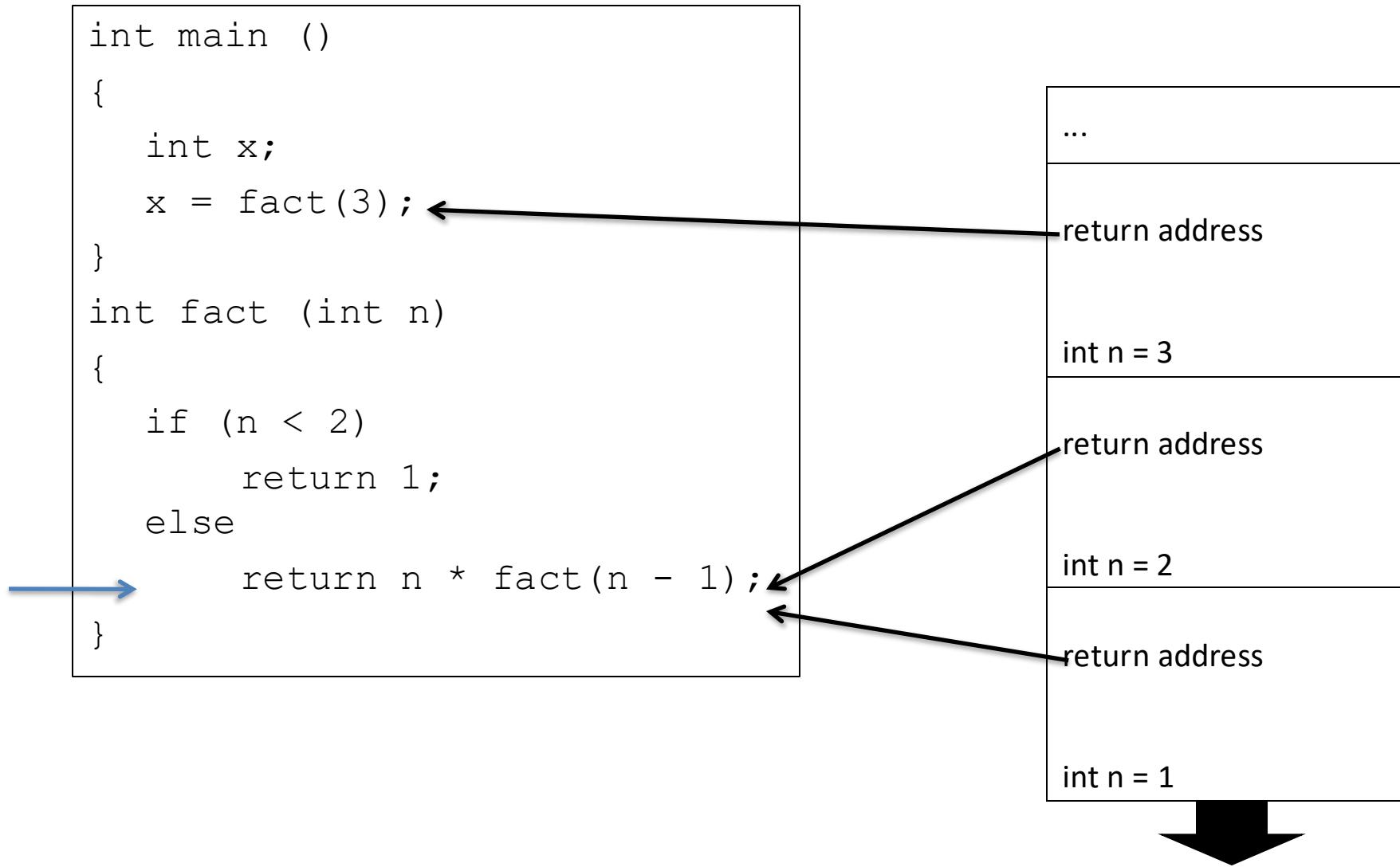


Process Stack

```
int main ()  
{  
    int x;  
    x = fact(3); ←  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        return n * fact(n - 1); ←  
}
```

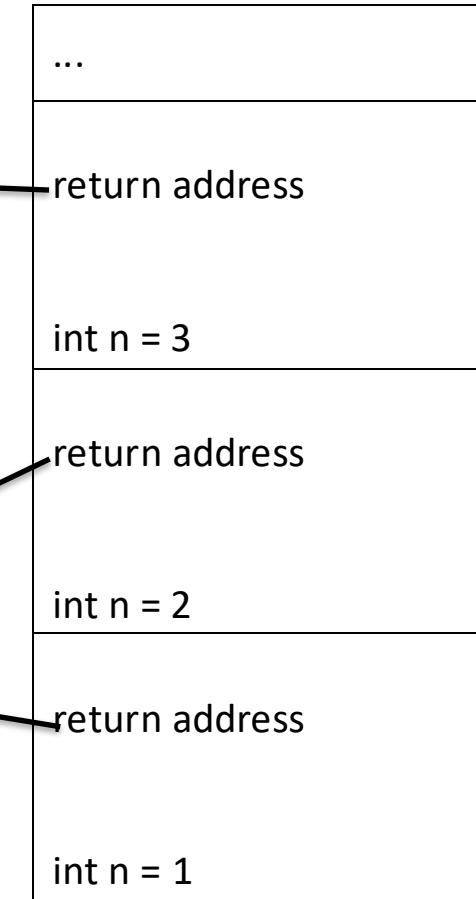


Process Stack



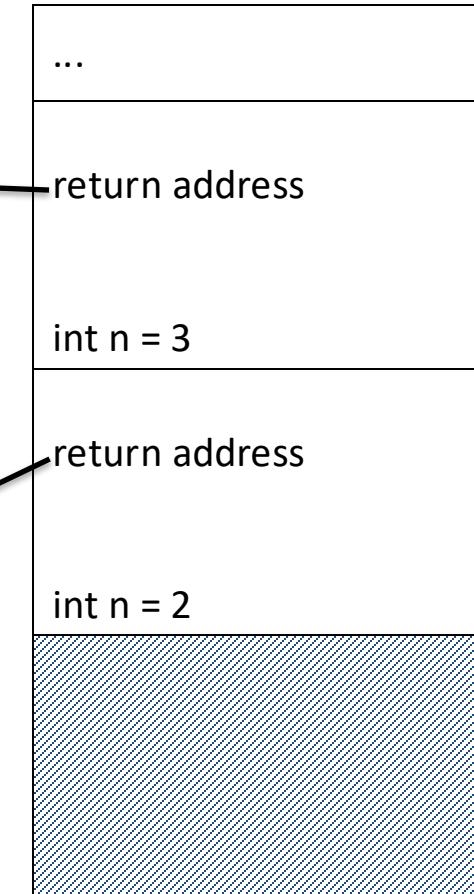
Process Stack

```
int main ()  
{  
    int x;  
    x = fact(3); ←  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        return n * fact(n - 1); ←  
}
```



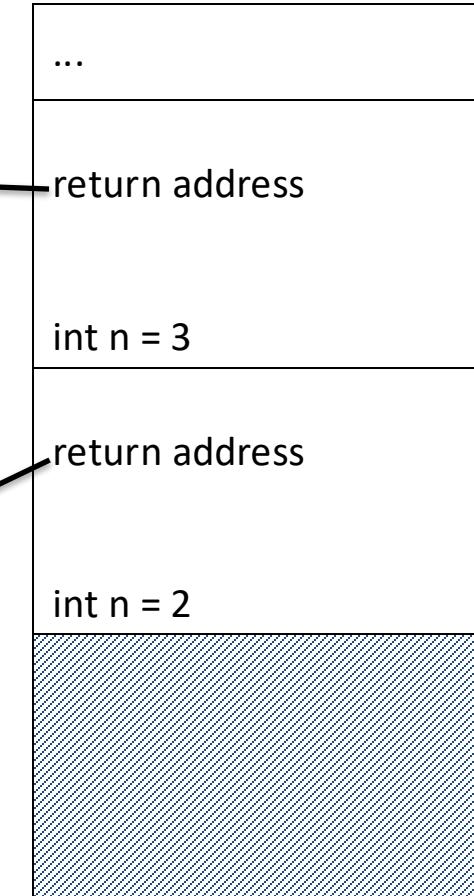
Process Stack

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    int x;  
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```



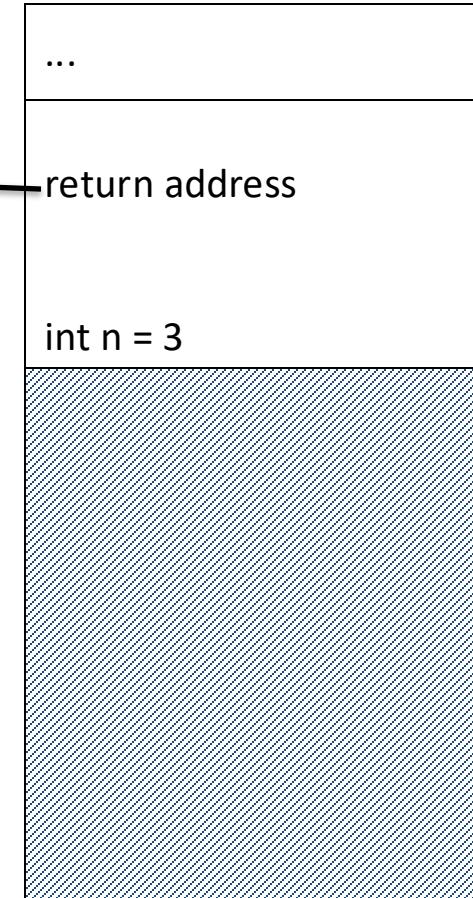
Process Stack

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    int x;  
    x = fact(3); ←  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        → return n * fact(n - 1); ←  
}
```



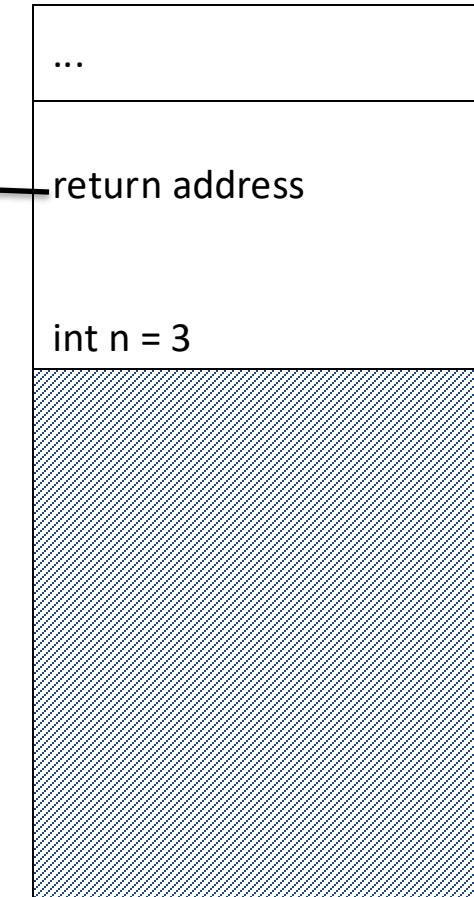
Process Stack

```
int main ()  
{  
    int x;  
    x = fact(3); ←  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        → return n * fact(n - 1); ← $ra  
}
```



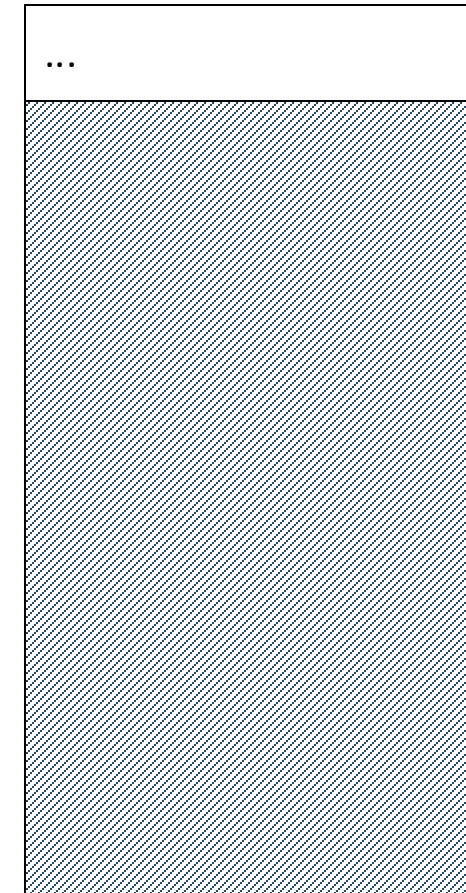
Process Stack

```
int main ()  
{  
    int x;  
    x = fact(3); ←  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        return n * fact(n - 1);  
}
```



Process Stack

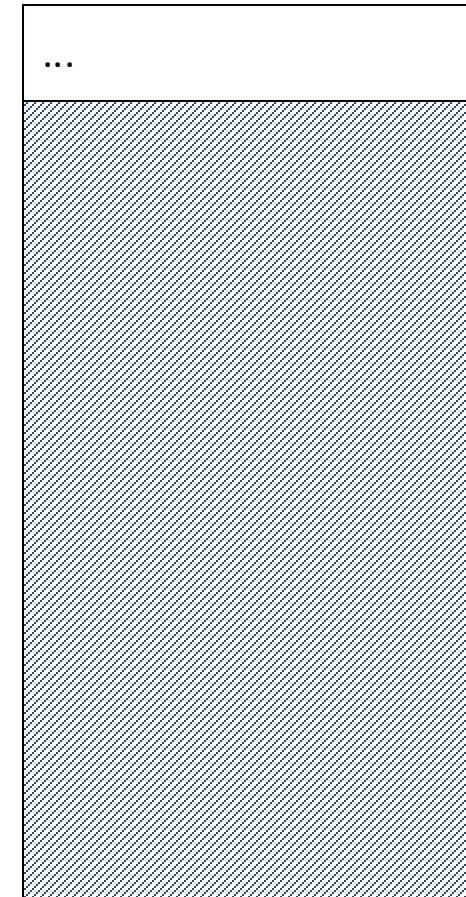
```
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{  
    int x;  
    x = fact(3); ← $ra  
}  
  
int fact (int n)  
{  
    if (n < 2)  
        return 1;  
    else  
        → return n * fact(n - 1);  
}
```



Process Stack

```
int main ()
{
    int x;
    → x = fact(3);
}

int fact (int n)
{
    if (n < 2)
        return 1;
    else
        return n * fact(n - 1);
}
```



Questions?

Non-Leaf Procedure Example

- MIPS code:

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)       # save argument
    slti $t0, $a0, 2        # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1      # if so, result is 1
    addi $sp, $sp, 8        # pop 2 items from stack
    jr   $ra                # and return
L1: addi $a0, $a0, -1      # else decrement n
    jal  fact              # recursive call
    lw   $a0, 4($sp)       # restore original n
    lw   $ra, 8($sp)       # and return address
    addi $sp, $sp, 8        # pop 2 items from stack
    mul  $v0, $a0, $v0      # multiply to get result
    jr   $ra                # and return
```

fact(3)

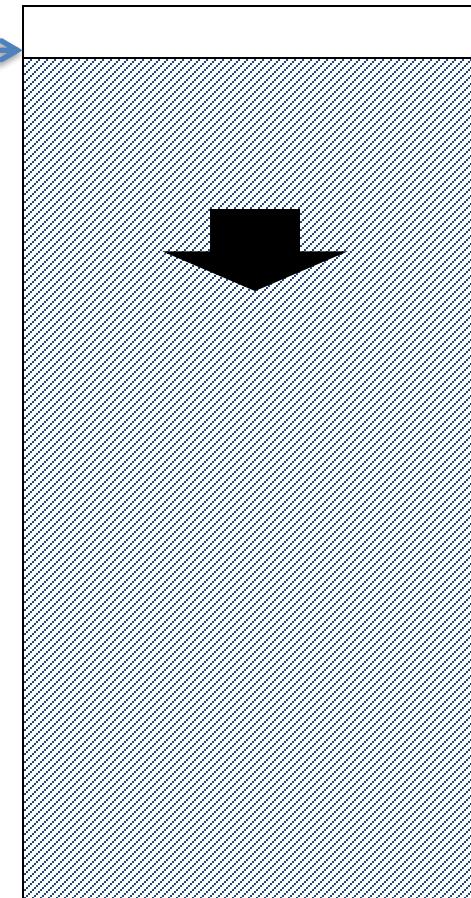
```
$ra = 0x864  
$a0 = 3  
$v0 =  
$t0 =
```

PC →

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)       # save argument
    slti $t0, $a0, 2       # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1     # if so, result is 1
    addi $sp, $sp, 8       # pop 2 items from stack
    jr   $ra               # and return
L1:  addi $a0, $a0, -1   # else decrement n
    jal   fact             # recursive call
    lw    $a0, 4($sp)       # restore original n
    lw    $ra, 8($sp)       # and return address
    addi $sp, $sp, 8       # pop 2 items from stack
    mul  $v0, $a0, $v0     # multiply to get result
    jr   $ra               # and return
```

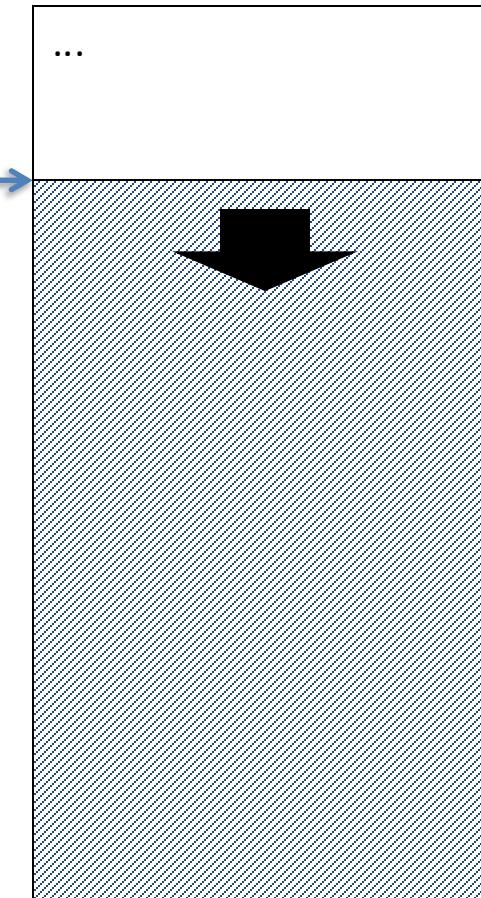
SP →



fact

```
$ra = 0x864  
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```

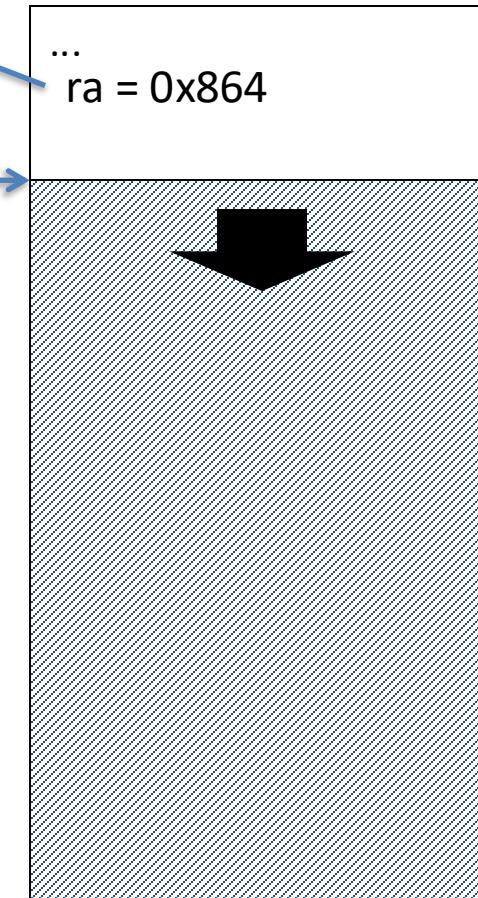
```
fact:  
PC → addi $sp, $sp, -8      # adjust stack for 2 items  
      sw    $ra, 8($sp)        # save return address  
      sw    $a0, 4($sp)        # save argument  
      slti $t0, $a0, 2         # test for n < 2  
      beq   $t0, $zero, L1  
      addi $v0, $zero, 1       # if so, result is 1  
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L1:  addi $a0, $a0, -1        # else decrement n  
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      lw    $a0, 4($sp)        # restore original n  
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```



fact

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$ra = 0x864  
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```

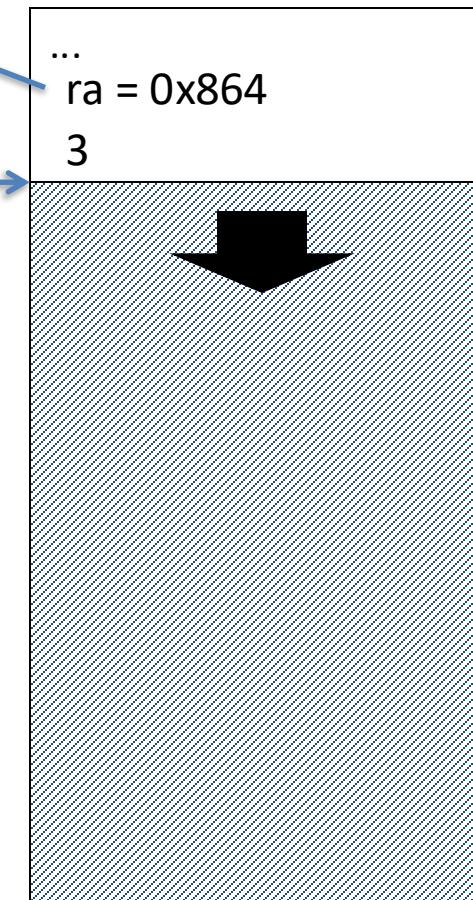
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    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra               # and return  
L1:  addi $a0, $a0, -1    # else decrement n  
    jal  fact              # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
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fact

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$ra = 0x864  
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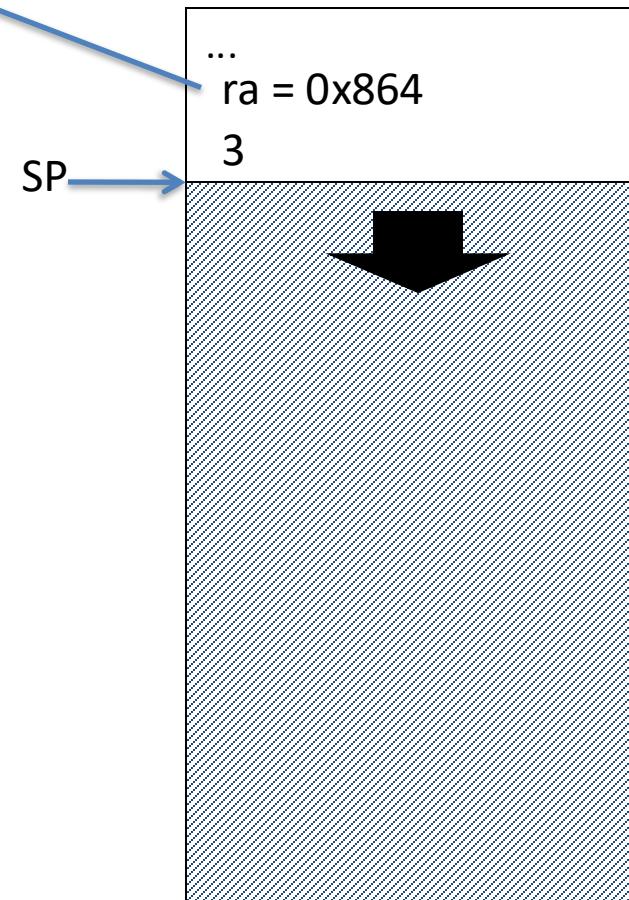
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw    $ra, 8($sp)       # save return address  
    PC → sw    $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq   $t0, $zero, L1  
    addi $v0, $zero, 1        # if so, result is 1  
    addi $sp, $sp, 8          # pop 2 items from stack  
    jr    $ra                  # and return  
L1:  addi $a0, $a0, -1        # else decrement n  
    jal   fact                # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8          # pop 2 items from stack  
    mul   $v0, $a0, $v0        # multiply to get result  
    jr    $ra                  # and return
```



fact

```
$ra = 0x864  
$a0 = 3  
$v0 =  
$t0 = 0
```

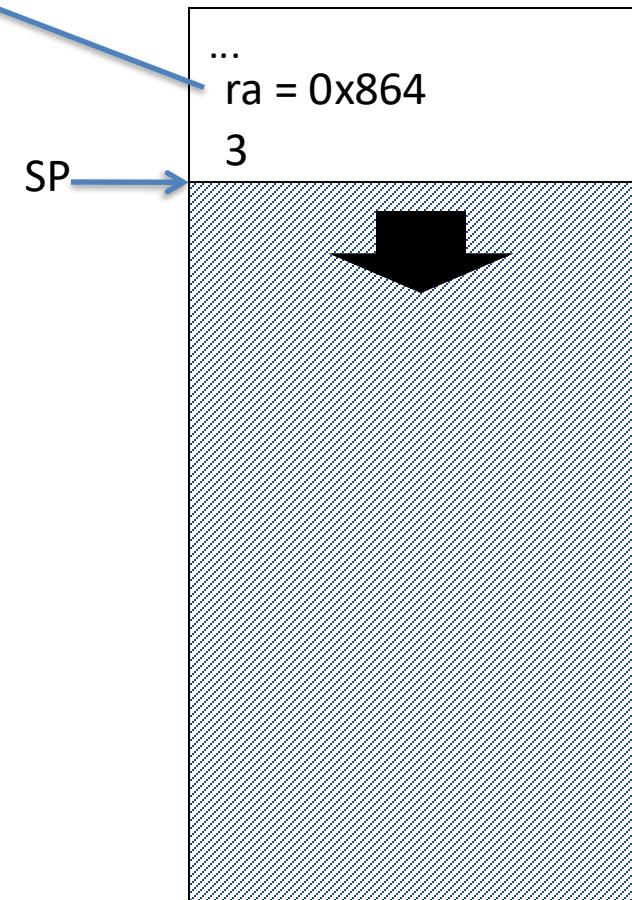
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    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
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    lw   $ra, 8($sp)        # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```



fact

```
$ra = 0x864  
$a0 = 3  
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$t0 = 0
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra               # and return  
L1:  addi $a0, $a0, -1    # else decrement n  
    jal  fact              # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8       # pop 2 items from stack  
    mul $v0, $a0, $v0      # multiply to get result  
    jr   $ra               # and return
```



fact

\$ra = 0x864

\$a0 = 2

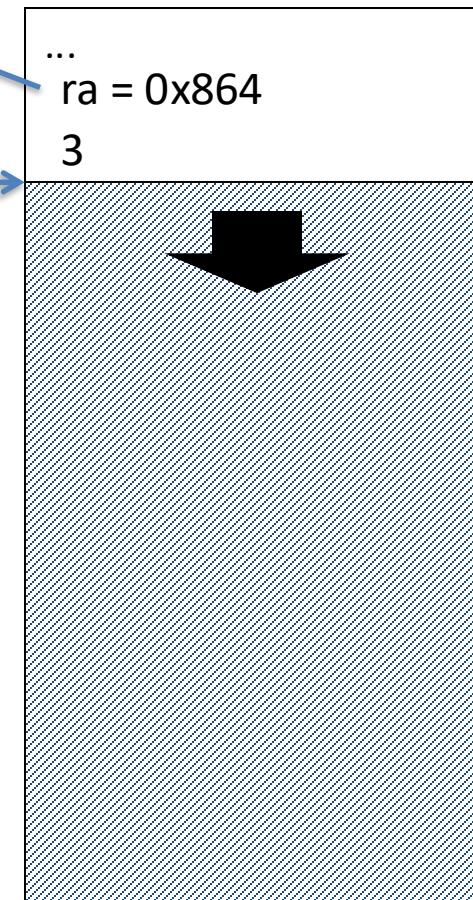
\$v0 =

\$t0 = 0

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)        # save argument
    slti $t0, $a0, 2        # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1      # if so, result is 1
    addi $sp, $sp, 8         # pop 2 items from stack
    jr   $ra                 # and return
PC  L1: addi $a0, $a0, -1      # else decrement n
      jal  fact              # recursive call
      lw   $a0, 4($sp)        # restore original n
      lw   $ra, 8($sp)        # and return address
      addi $sp, $sp, 8         # pop 2 items from stack
      mul  $v0, $a0, $v0        # multiply to get result
      jr   $ra                 # and return
```

SP



After this line of code, the next line of code we run will be

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq $t0, $zero, L1  
    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra                # and return  
L1: addi $a0, $a0, -1      # else decrement n  
    jal fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8       # pop 2 items from stack  
    mul $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```

PC →

```
$ra = 0x864  
$a0 = 2  
$v0 =  
$t0 = 0
```

- A. lw \$a0, 4(\$sp)
- B. addi \$a0, \$a0, -1
- C. addi \$sp, \$sp, -8
- D. jr \$ra
- E. None of the above

fact

\$ra = L1 + 8

\$a0 = 2

\$v0 =

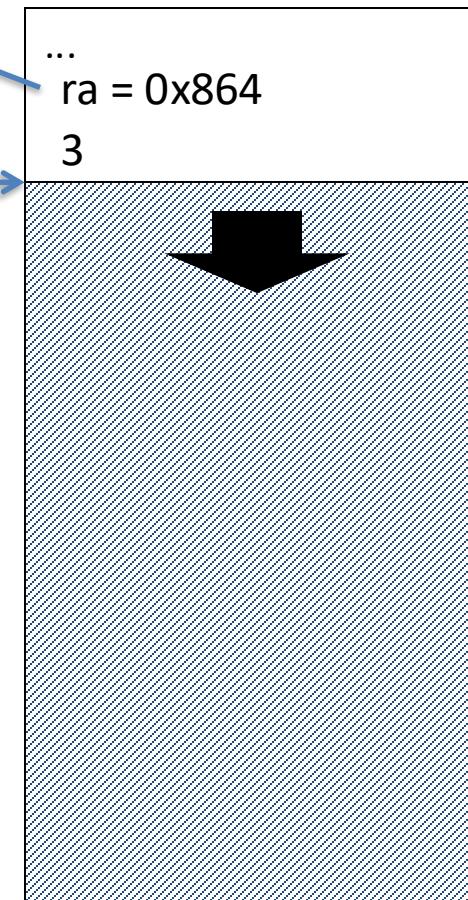
\$t0 = 0

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)       # save argument
    slti $t0, $a0, 2        # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1      # if so, result is 1
    addi $sp, $sp, 8        # pop 2 items from stack
    jr   $ra                # and return
L1:  addi $a0, $a0, -1      # else decrement n
    jal  fact              # recursive call
    lw   $a0, 4($sp)       # restore original n
    lw   $ra, 8($sp)       # and return address
    addi $sp, $sp, 8        # pop 2 items from stack
    mul  $v0, $a0, $v0      # multiply to get result
    jr   $ra                # and return
```

PC

SP



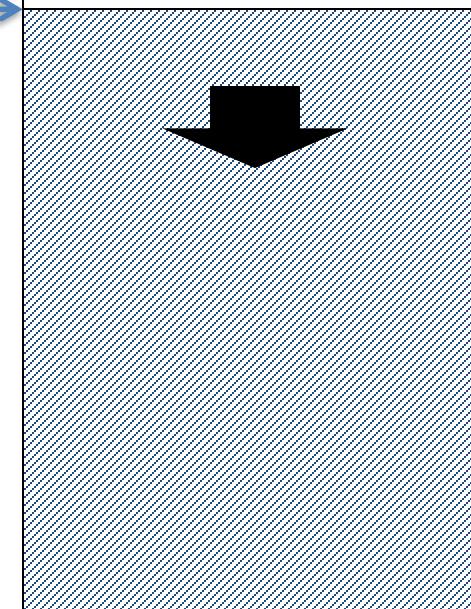
fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 =  
$t0 =
```

```
fact:  
PC → addi $sp, $sp, -8      # adjust stack for 2 items  
      sw    $ra, 8($sp)        # save return address  
      sw    $a0, 4($sp)        # save argument  
      slti $t0, $a0, 2         # test for n < 2  
      beq   $t0, $zero, L1  
      addi $v0, $zero, 1       # if so, result is 1  
      addi $sp, $sp, 8          # pop 2 items from stack  
      jr    $ra                 # and return  
L1:  addi $a0, $a0, -1        # else decrement n  
      jal   fact                # recursive call  
      lw    $a0, 4($sp)        # restore original n  
      lw    $ra, 8($sp)        # and return address  
      addi $sp, $sp, 8          # pop 2 items from stack  
      mul   $v0, $a0, $v0       # multiply to get result  
      jr    $ra                 # and return
```

```
ra = 0x864  
3
```

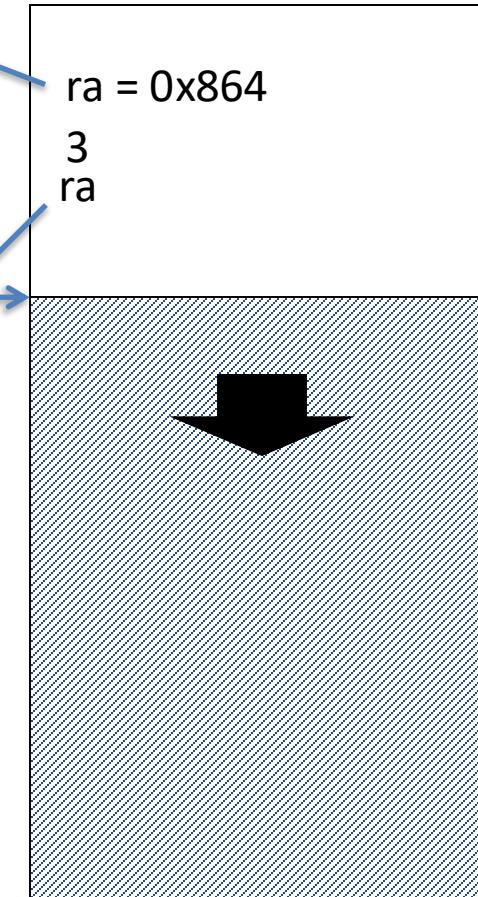
SP



fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 =  
$t0 = 0
```

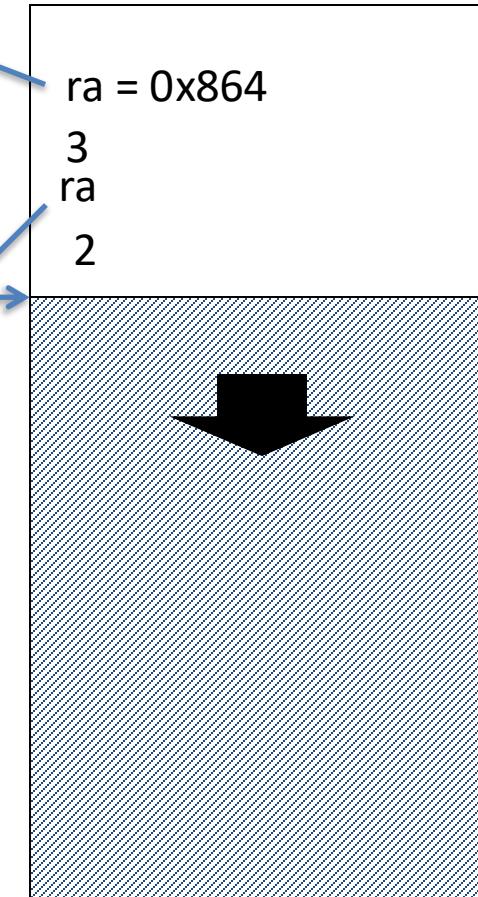
```
fact:  
PC    addi $sp, $sp, -8      # adjust stack for 2 items  
      sw   $ra, 8($sp)        # save return address  
      sw   $a0, 4($sp)        # save argument  
      slti $t0, $a0, 2        # test for n < 2  
      beq  $t0, $zero, L1  
      addi $v0, $zero, 1      # if so, result is 1  
      addi $sp, $sp, 8        # pop 2 items from stack  
      jr   $ra                # and return  
L1:   addi $a0, $a0, -1      # else decrement n  
      jal  fact              # recursive call  
      lw   $a0, 4($sp)        # restore original n  
      lw   $ra, 8($sp)        # and return address  
      addi $sp, $sp, 8        # pop 2 items from stack  
      mul  $v0, $a0, $v0      # multiply to get result  
      jr   $ra                # and return
```



fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 =  
$t0 = 0
```

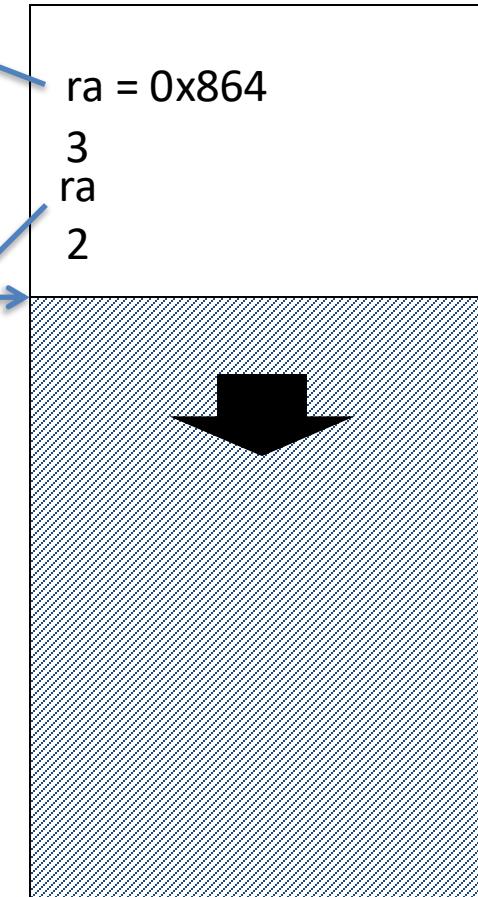
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw    $ra, 8($sp)       # save return address  
    PC → sw    $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq   $t0, $zero, L1  
    addi $v0, $zero, 1        # if so, result is 1  
    addi $sp, $sp, 8          # pop 2 items from stack  
    jr    $ra                  # and return  
L1:  addi $a0, $a0, -1        # else decrement n  
    jal   fact                # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8          # pop 2 items from stack  
    mul   $v0, $a0, $v0        # multiply to get result  
    jr    $ra                  # and return
```



fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 =  
$t0 = 0
```

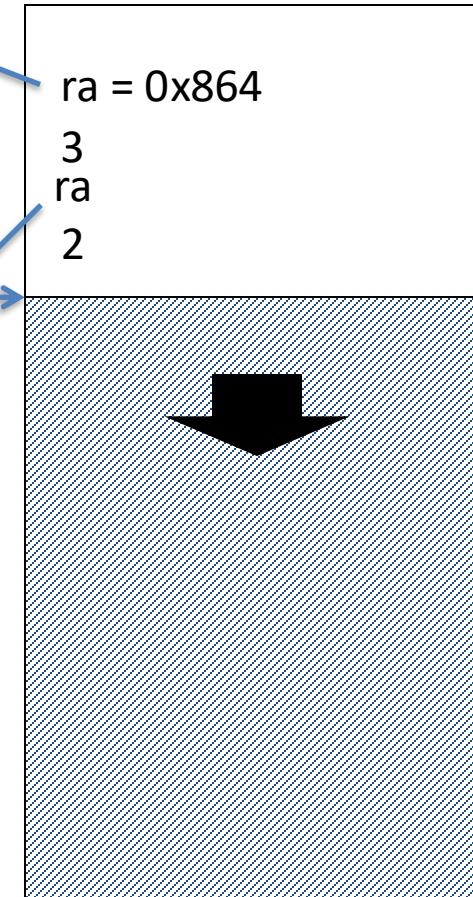
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)        # restore original n  
    lw   $ra, 8($sp)        # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```



fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 =  
$t0 = 0
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    PC → beq $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```



fact

\$ra = L1 + 8

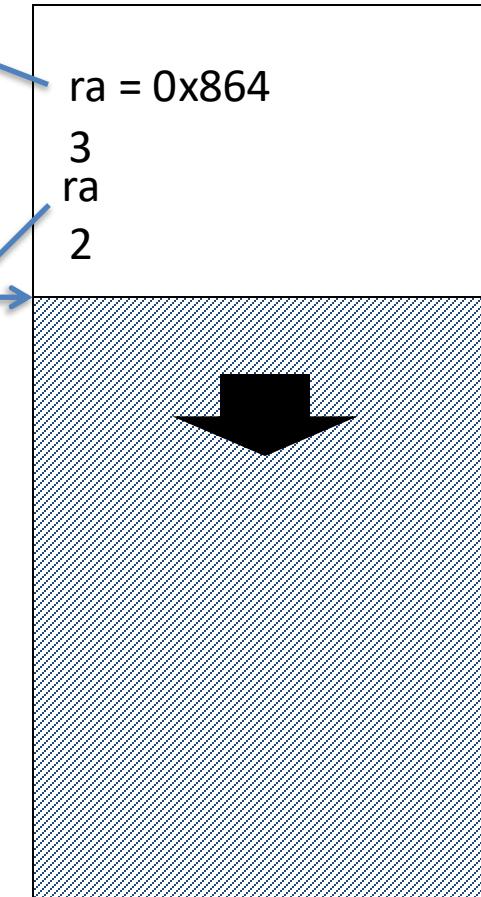
\$a0 = 1

\$v0 =

\$t0 = 0

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)       # save argument
    slti $t0, $a0, 2        # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1      # if so, result is 1
    addi $sp, $sp, 8        # pop 2 items from stack
    jr   $ra                # and return
PC  L1  addi $a0, $a0, -1  # else decrement n
    jal  fact              # recursive call
    lw   $a0, 4($sp)       # restore original n
    lw   $ra, 8($sp)       # and return address
    addi $sp, $sp, 8        # pop 2 items from stack
    mul  $v0, $a0, $v0      # multiply to get result
    jr   $ra                # and return
```

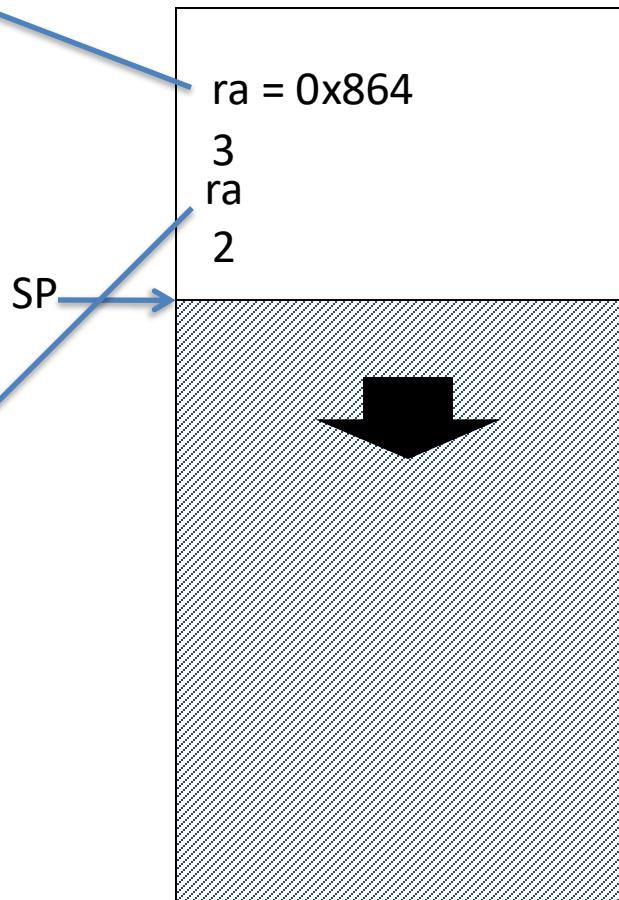


fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 =  
$t0 = 0
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```

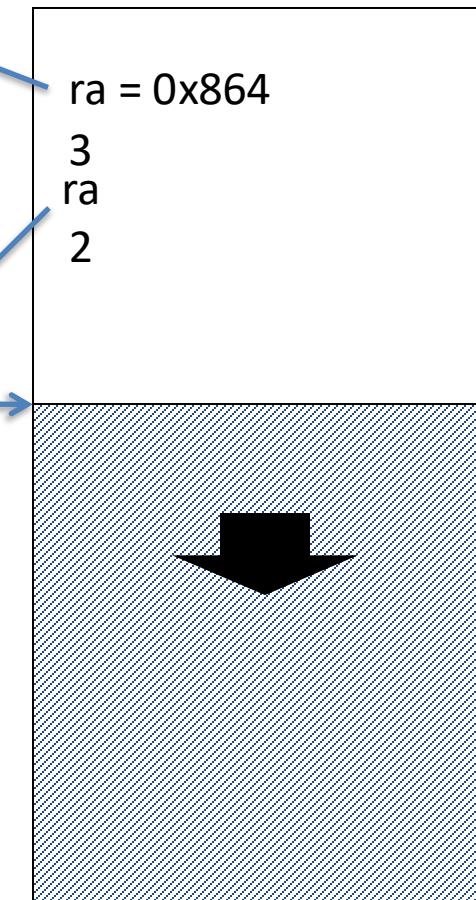
PC



fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 =  
$t0 = 0
```

```
fact:  
PC → addi $sp, $sp, -8      # adjust stack for 2 items  
    sw  $ra, 8($sp)          # save return address  
    sw  $a0, 4($sp)          # save argument  
    slti $t0, $a0, 2         # test for n < 2  
    beq $t0, $zero, L1  
    addi $v0, $zero, 1        # if so, result is 1  
    addi $sp, $sp, 8          # pop 2 items from stack  
    jr  $ra                  # and return  
L1: addi $a0, $a0, -1        # else decrement n  
    jal fact                 # recursive call  
    lw   $a0, 4($sp)          # restore original n  
    lw   $ra, 8($sp)          # and return address  
    addi $sp, $sp, 8          # pop 2 items from stack  
    mul $v0, $a0, $v0         # multiply to get result  
    jr  $ra                  # and return
```

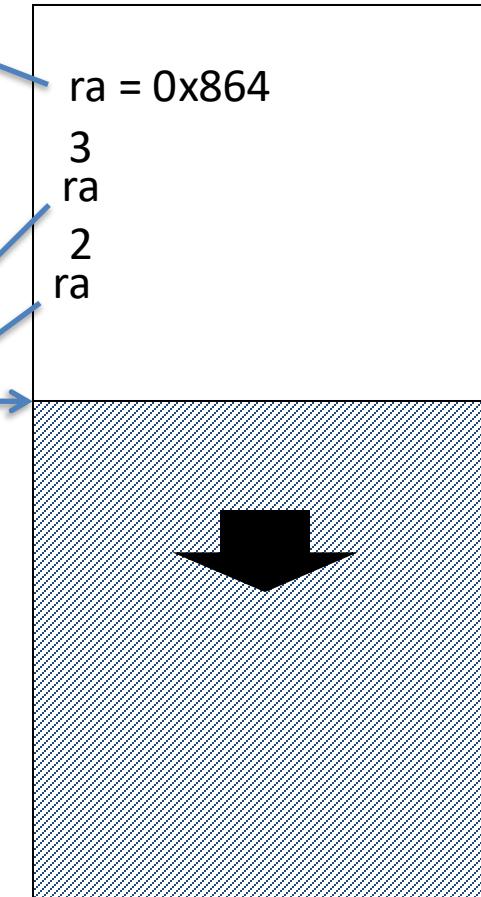


fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 =  
$t0 = 0
```

PC →

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```

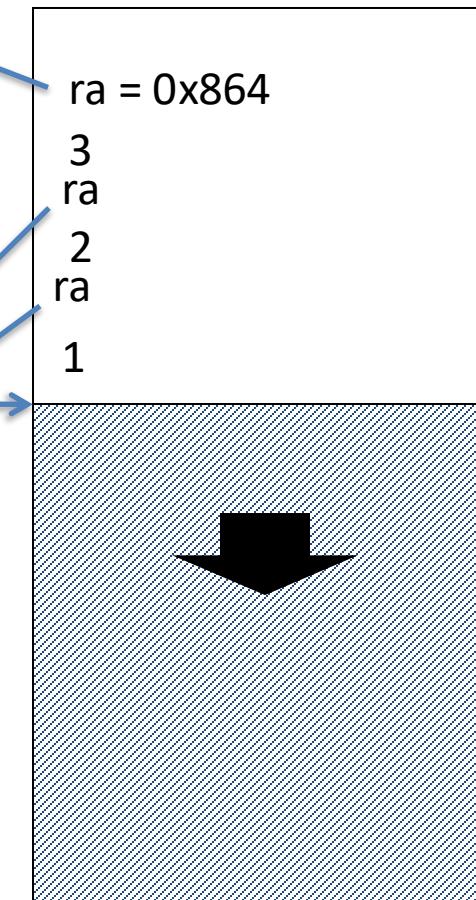


fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 =  
$t0 = 0
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw    $ra, 8($sp)       # save return address  
    sw    $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq   $t0, $zero, L1  
    addi $v0, $zero, 1        # if so, result is 1  
    addi $sp, $sp, 8         # pop 2 items from stack  
    jr    $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal   fact              # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8         # pop 2 items from stack  
    mul   $v0, $a0, $v0        # multiply to get result  
    jr    $ra                # and return
```

PC →

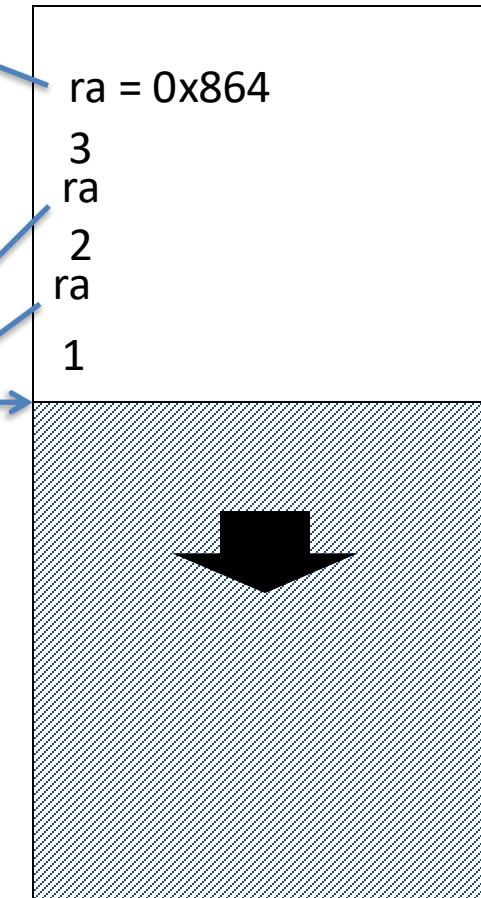


fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 =  
$t0 = 1
```

PC →

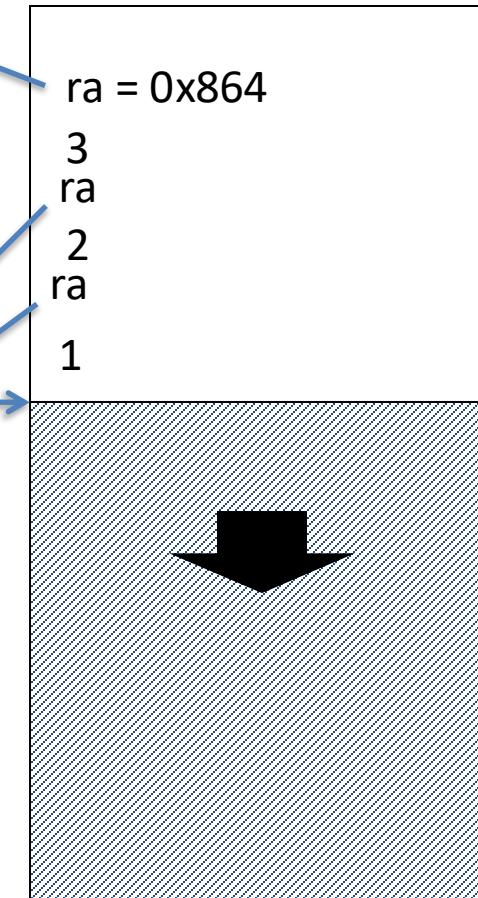
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)        # restore original n  
    lw   $ra, 8($sp)        # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```



fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 =  
$t0 = 1
```

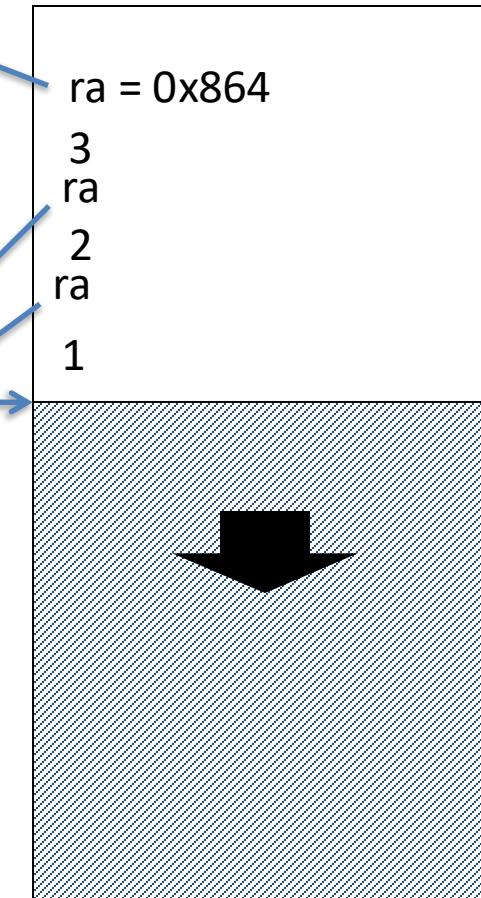
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    PC → beq $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```



fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 = 1  
$t0 = 1
```

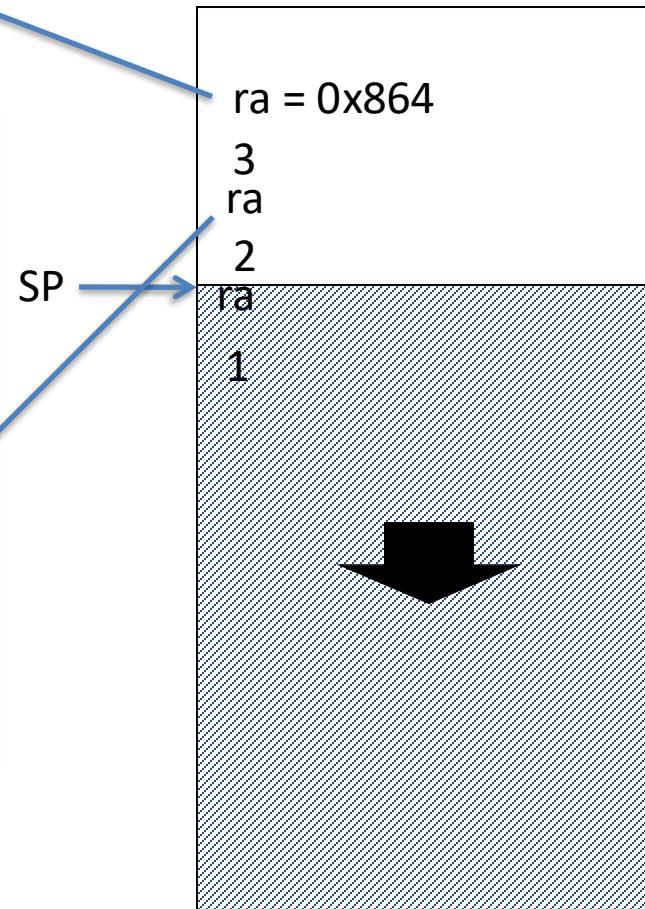
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    PC → addi $v0, $zero, 1 # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```



```
$ra = L1 + 8  
$a0 = 1  
$v0 = 1  
$t0 = 1
```

fact

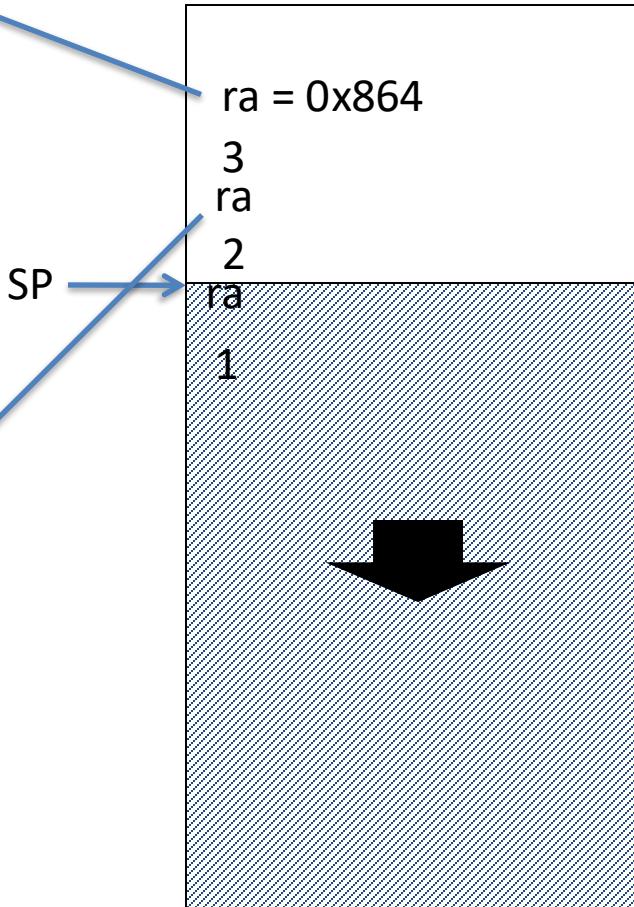
```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal   fact              # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul   $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```



fact

```
$ra = L1 + 8  
$a0 = 1  
$v0 = 1  
$t0 = 1
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal   fact              # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```



```
$ra = L1 + 8
$a0 = 1
$v0 = 1
$t0 = 1
```

We will return to

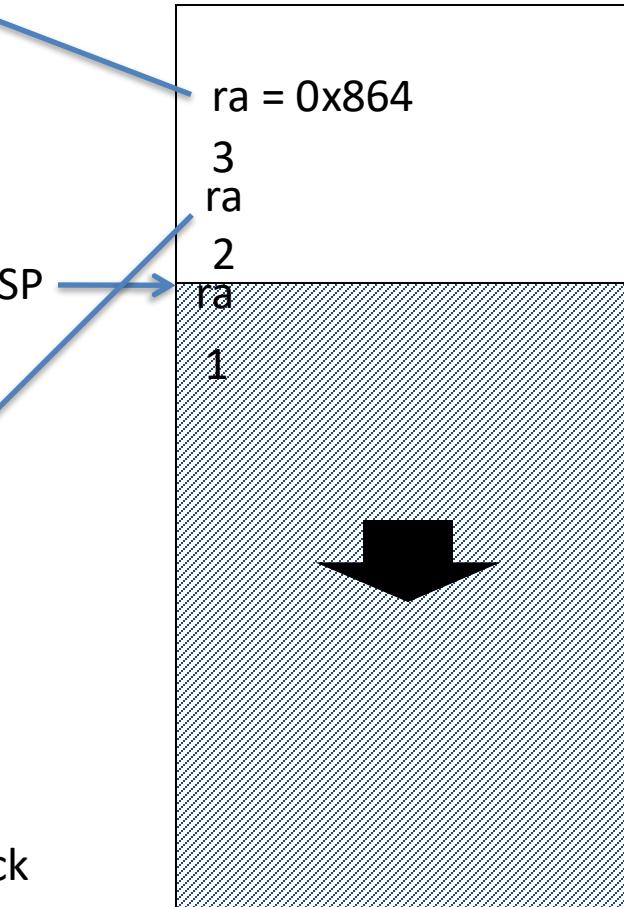
fact:

```

addi $sp, $sp, -8      # adjust stack for 2 items
sw   $ra, 8($sp)       # save return address
sw   $a0, 4($sp)        # save argument
slti $t0, $a0, 2        # test for n < 2
beq  $t0, $zero, L1
addi $v0, $zero, 1      # if so, result is 1
addi $sp, $sp, 8         # pop 2 items from stack
jr   $ra                 # and return
L1: addi $a0, $a0, -1    # else decrement n
jal   fact               # recursive call
lw    $a0, 4($sp)        # restore original n
lw    $ra, 8($sp)        # and return address
addi $sp, $sp, 8         # pop 2 items from stack
mul  $v0, $a0, $v0        # multiply to get result
jr   $ra                 # and return

```

PC → L1:



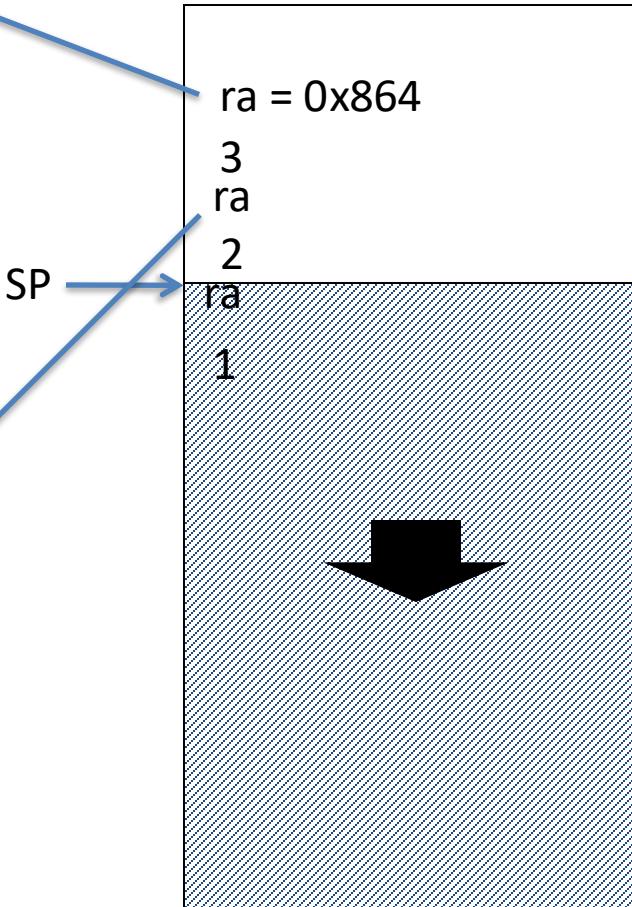
- A. L1 + 8, because it's in \$ra
- B. L1 + 8, because it's the most recent value on the stack
- C. 0x864, because it's the top value on the stack
- D. fact, because it's the procedure call
- E. None of the above

fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 = 1  
$t0 = 1
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal   fact              # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```

PC →



fact

\$ra = L1 + 8

\$a0 = 2

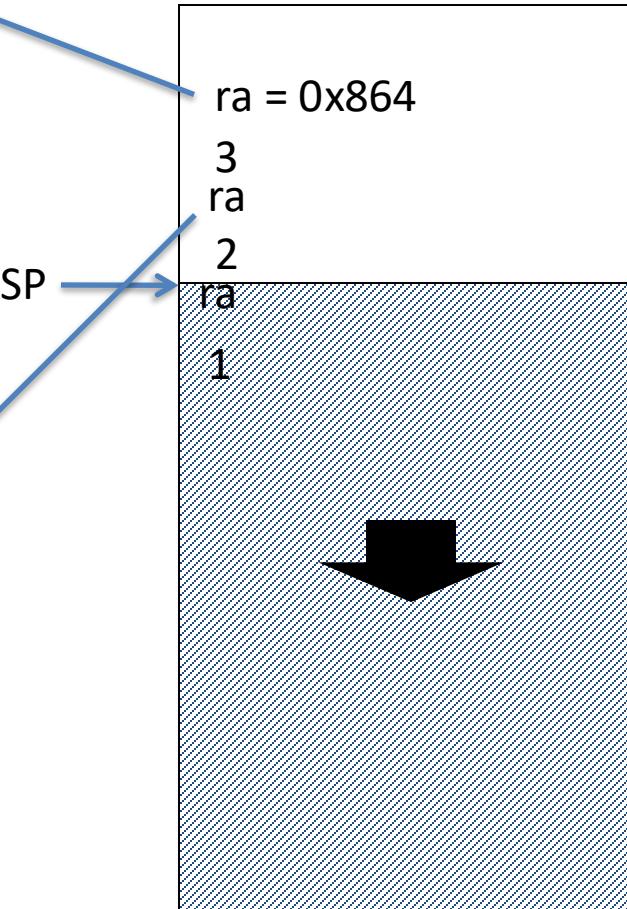
\$v0 = 1

\$t0 = 1

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)       # save argument
    slti $t0, $a0, 2        # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1      # if so, result is 1
    addi $sp, $sp, 8        # pop 2 items from stack
    jr   $ra                # and return
L1:  addi $a0, $a0, -1      # else decrement n
    jal   fact              # recursive call
    lw    $a0, 4($sp)       # restore original n
    lw    $ra, 8($sp)       # and return address
    addi $sp, $sp, 8        # pop 2 items from stack
    mul  $v0, $a0, $v0      # multiply to get result
    jr   $ra                # and return
```

PC

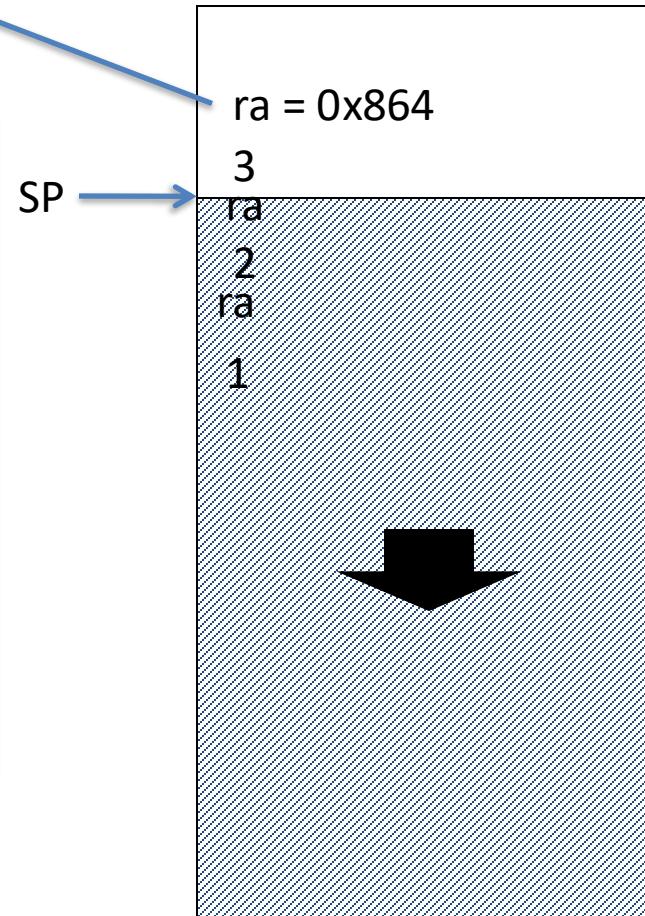


fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 = 1  
$t0 = 1
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra               # and return  
L1:  addi $a0, $a0, -1    # else decrement n  
    jal   fact             # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8       # pop 2 items from stack  
    mul   $v0, $a0, $v0     # multiply to get result  
    jr   $ra               # and return
```

PC

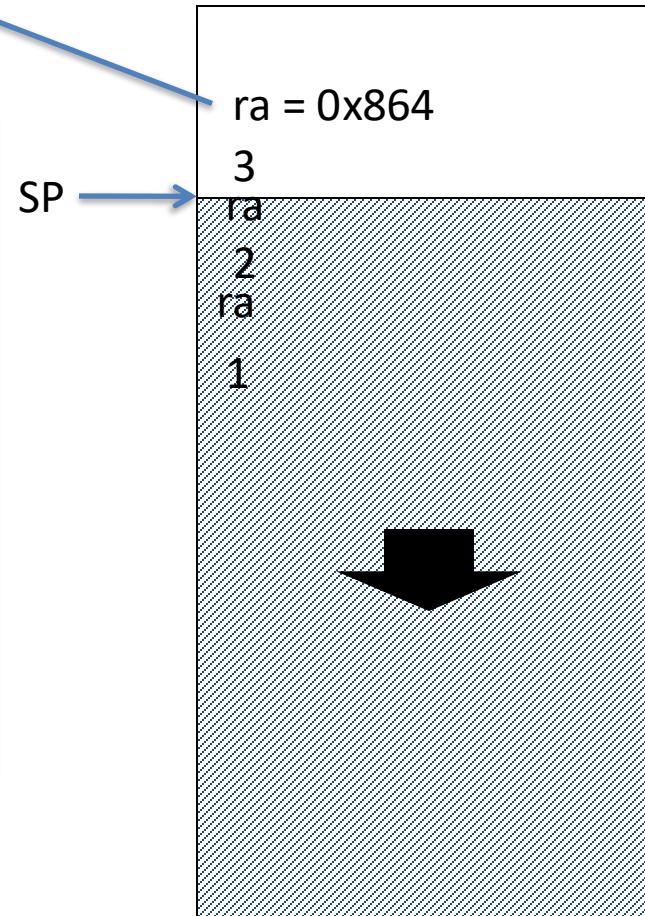


```
$ra = L1 + 8  
$a0 = 2  
$v0 = 2  
$t0 = 1
```

fact

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra               # and return  
L1:  addi $a0, $a0, -1    # else decrement n  
    jal  fact              # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8       # pop 2 items from stack  
    mul  $v0, $a0, $v0     # multiply to get result  
    jr   $ra               # and return
```

PC

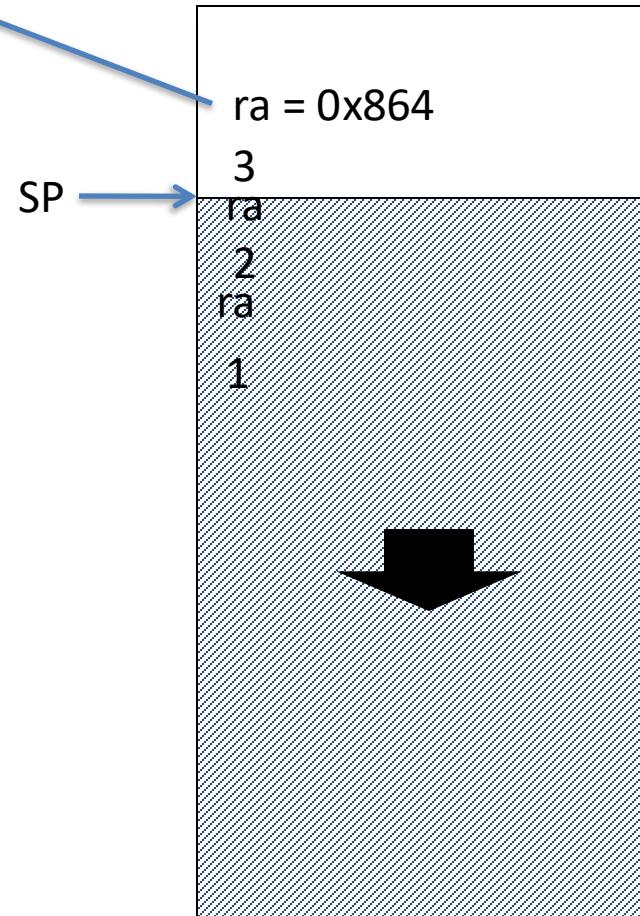


fact

```
$ra = L1 + 8  
$a0 = 2  
$v0 = 2  
$t0 = 1
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra               # and return  
L1:  addi $a0, $a0, -1    # else decrement n  
    jal   fact             # recursive call  
    lw    $a0, 4($sp)       # restore original n  
    lw    $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8       # pop 2 items from stack  
    mul   $v0, $a0, $v0     # multiply to get result  
    jr   $ra               # and return
```

PC

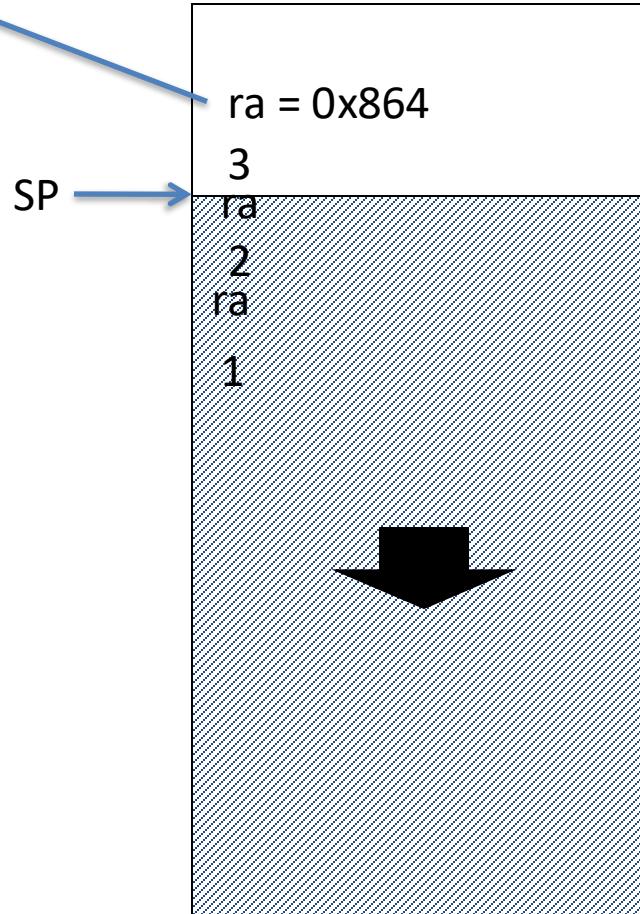


fact

```
$ra = L1 + 8  
$a0 = 3  
$v0 = 2  
$t0 = 1
```

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal   fact              # recursive call  
    lw    $a0, 4($sp)        # restore original n  
    lw    $ra, 8($sp)        # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0       # multiply to get result  
    jr   $ra                # and return
```

PC



\$ra = 0x864

\$a0 = 3

\$v0 = 2

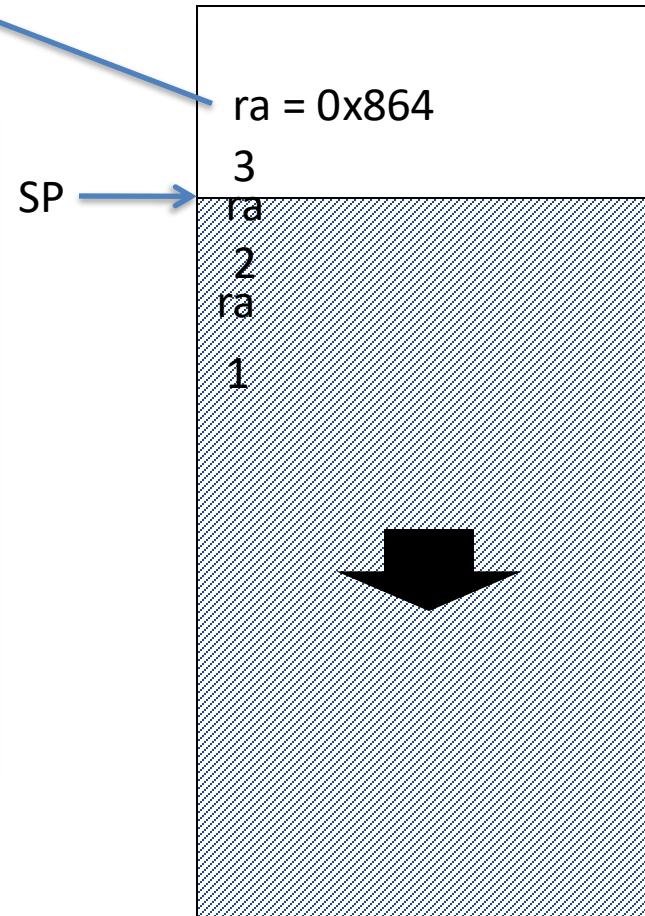
\$t0 = 1

fact

fact:

```
    addi $sp, $sp, -8      # adjust stack for 2 items
    sw   $ra, 8($sp)       # save return address
    sw   $a0, 4($sp)       # save argument
    slti $t0, $a0, 2       # test for n < 2
    beq  $t0, $zero, L1
    addi $v0, $zero, 1     # if so, result is 1
    addi $sp, $sp, 8       # pop 2 items from stack
    jr   $ra               # and return
L1:  addi $a0, $a0, -1   # else decrement n
    jal   fact             # recursive call
    lw    $a0, 4($sp)       # restore original n
    lw    $ra, 8($sp)       # and return address
    addi $sp, $sp, 8       # pop 2 items from stack
    mul   $v0, $a0, $v0     # multiply to get result
    jr   $ra               # and return
```

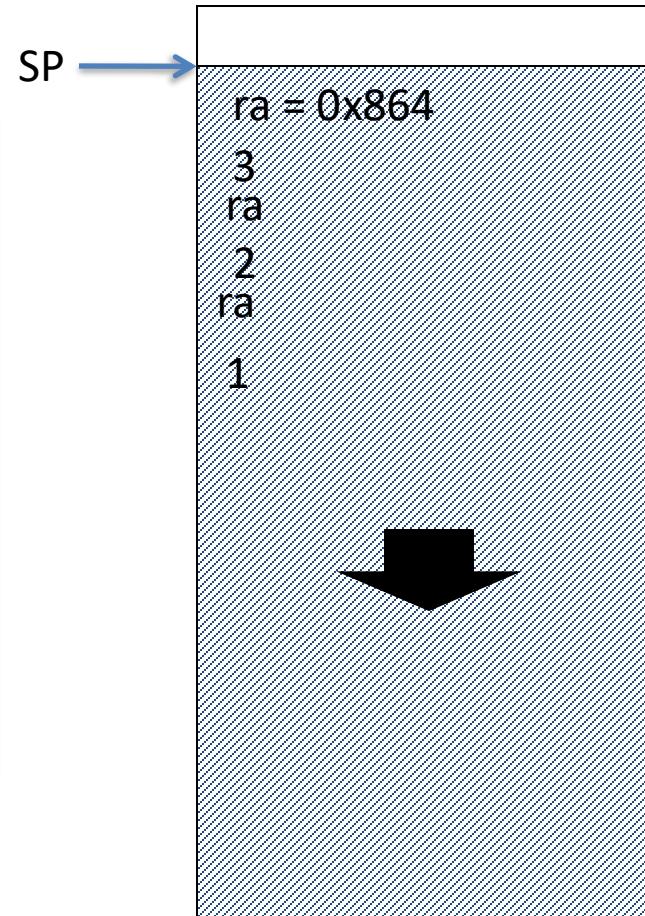
PC



```
$ra = 0x864  
$a0 = 3  
$v0 = 2  
$t0 = 1
```

fact

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2       # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1     # if so, result is 1  
    addi $sp, $sp, 8       # pop 2 items from stack  
    jr   $ra               # and return  
L1:  addi $a0, $a0, -1    # else decrement n  
    jal  fact              # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    PC → addi $sp, $sp, 8    # pop 2 items from stack  
    mul  $v0, $a0, $v0      # multiply to get result  
    jr   $ra               # and return
```



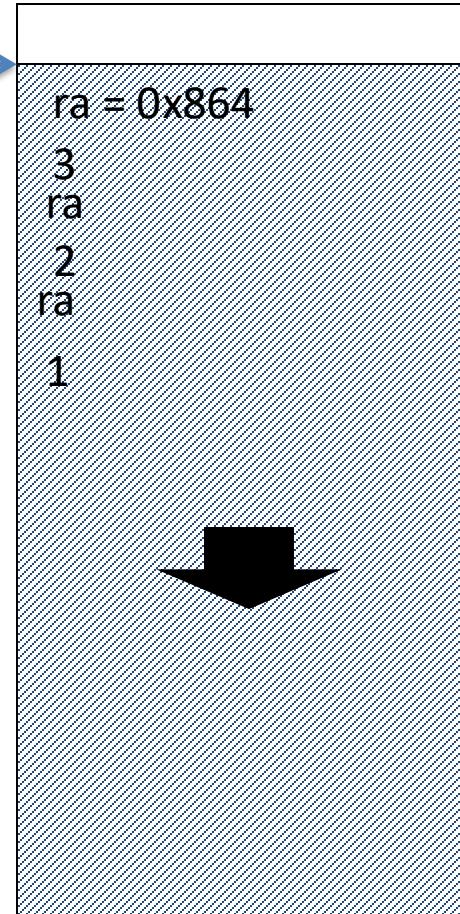
```
$ra = 0x864  
$a0 = 3  
$v0 = 6  
$t0 = 1
```

fact

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact               # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```

PC

SP



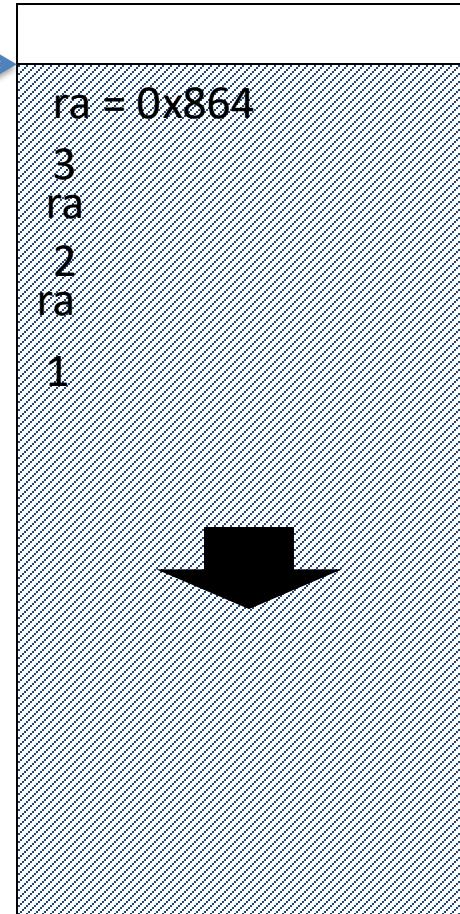
```
$ra = 0x864  
$a0 = 3  
$v0 = 6  
$t0 = 1
```

fact

```
fact:  
    addi $sp, $sp, -8      # adjust stack for 2 items  
    sw   $ra, 8($sp)       # save return address  
    sw   $a0, 4($sp)       # save argument  
    slti $t0, $a0, 2        # test for n < 2  
    beq  $t0, $zero, L1  
    addi $v0, $zero, 1      # if so, result is 1  
    addi $sp, $sp, 8        # pop 2 items from stack  
    jr   $ra                # and return  
L1:  addi $a0, $a0, -1      # else decrement n  
    jal  fact                # recursive call  
    lw   $a0, 4($sp)       # restore original n  
    lw   $ra, 8($sp)       # and return address  
    addi $sp, $sp, 8        # pop 2 items from stack  
    mul  $v0, $a0, $v0      # multiply to get result  
    jr   $ra                # and return
```

PC

SP



Why store registers relative to the stack pointer,
rather than at some set memory location?

- A. Saves space.
- B. Easier to figure out where we stored things.
- C. Functions won't overwrite each other's saves.
- D. None of the above

Assembler directives

- Instructions to the assembler
 - .data / .text / .rodata / .bss are used to switch between global (mutable) data, executable code, read-only data, and uninitialized data in the output
 - .word x allocates space for 4 bytes with value x
 - .space n allocates n bytes of space
 - .asciiz “string” writes a 0-terminated string at that location

Review: Arrays!

- How do we declare a 10-word array in our data section?
- Could do

```
.data  
x1:    .word  0  
x2:    .word  0  
x3:    .word  0  
...  
x10:   .word  0
```

Review: Declaring an Array

- Instead, just declare a big chunk of memory

```
.data  
arr: .space 40
```

```

.data
arr:    .space 40

.text
    li      $t0, 0
    addi   $t1, $t0, 10
    la     $s0, arr
loop:
    beq    $t0, $t1, end
    What goes here?
    addi   $t0, $t0, 1
    j      loop
end:

```

D. More than one of the above

E. None of the above

```

int i;
for (i = 0; i < 10; i++){
    arr[i] = i;
}

```

sw \$t0, \$t1(\$s0)

A

```

add    $t2, $s0, $t1
sw      $t0, 0($t2)

```

B

sw \$t0, 0(\$s0)
addi \$s0, \$s0, 4

C

But what if we don't know how big the array will be before runtime?

sbrk system call

- Allocates memory and returns its address in \$v0
- Amount of memory is specified in bytes in \$a0
- Used by malloc, new

System Calls

- Syscalls (when we need OS intervention)
 - I/O (print/read stdout/file)
 - Exit (terminate)
 - Get system time
 - Random values

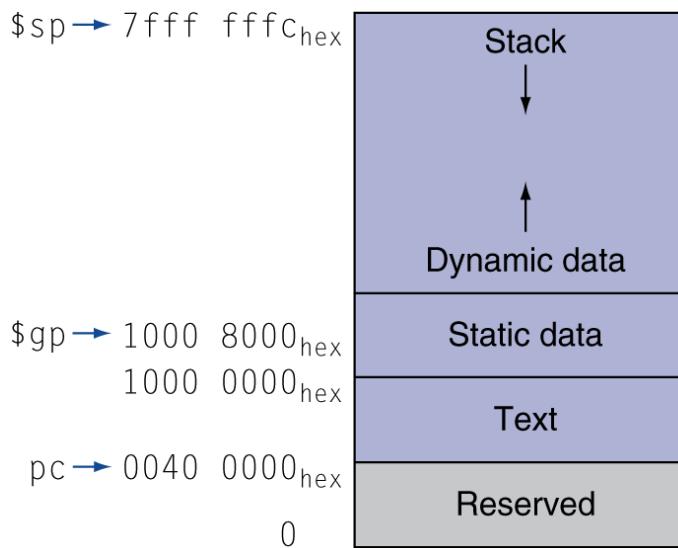
System Calls Review

- How to use:
 - Put syscall number into register \$v0
 - Load arguments into argument registers
 - Issue syscall instruction
 - Retrieve return values
- Example (allocate \$t4 bytes of memory with sbrk):

```
li      $v0, 9      # sbrk system call number
move   $a0, $t4# allocate $t4 bytes of mem
syscall
move   $s0, $v0# $s0 holds a pointer to mem
```

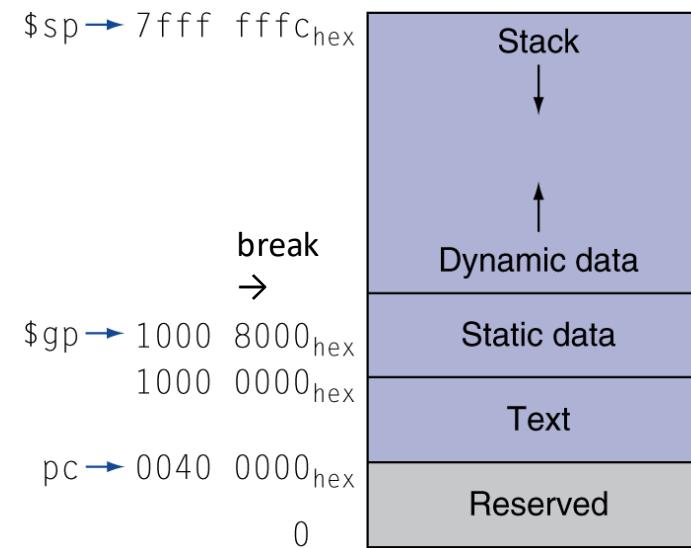
sbrk allocates memory from which region?

- A. Stack
- B. Dynamic data
- C. Static data
- D. Text
- E. Reserved



What about freeing memory?

- Some operating systems maintain a “program break” which controls the size of the dynamic data
- sbrk requests the OS increment/decrement the break
- malloc()/free() carve the dynamic data up into chunks which the application can use and maintain lists of free chunks
- Freeing memory adds the chunk to a “free list”
- When more memory is needed, the break is changed



Reading

- Next lecture: More Stack
- Problem set 3 due Today
- Lab 2 due Sunday